# Evolutionary Optimization Approach towards Unraveling High-Resolution X-ray Imaging and Spectroscopic Studies of High-Energy Astrophysical Sources



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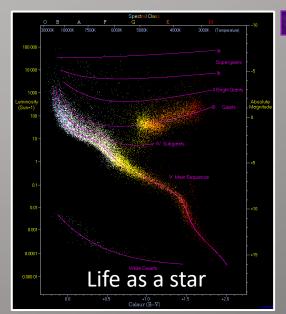


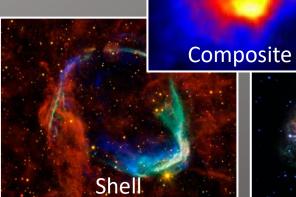
# Supernovae









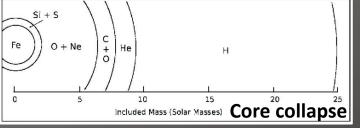




# ... and their Remnants

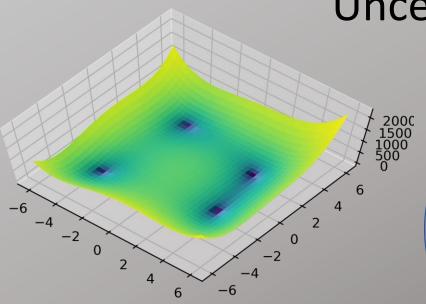








**Uncertainty & Degeneracy** 



#### **Systematic Uncertainty**

**Model Approximations** 

Spectral Database

Fitting Technique

Spatial/Spectral Resolution

#### **Random Uncertainty** (Noise)

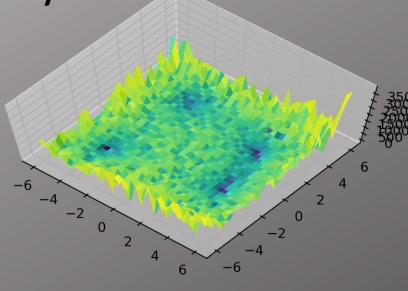
**Detector Background** 

**Soft Proton Flares** 

Readout noise

Charge-pileup

Cosmic Rays



Flattening/Broadening Narrowing/Jagged features Insensitivity to fit

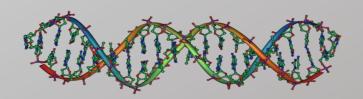


### **Objective (fitness) function**

Chi-squared:  $\chi^2 = \sum_i \frac{[N_{i,S} - M_i(x_i, p_B, p_S)]^2}{\sigma_i^2}$ 

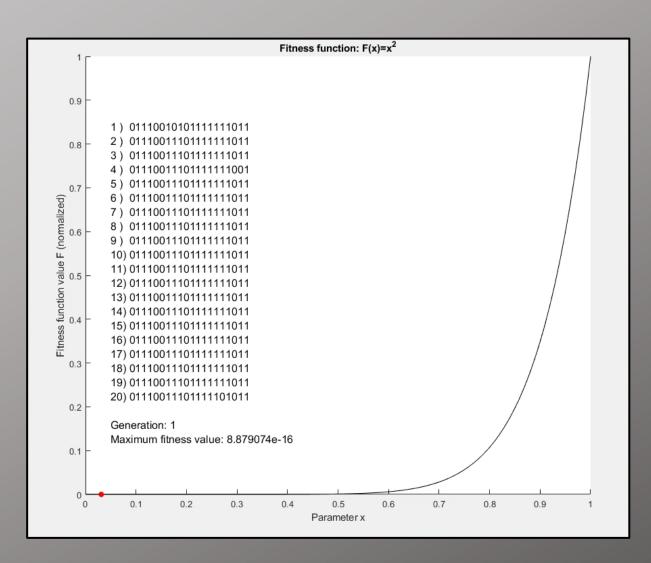
C-stat:  $C = 2\sum_{i} [M_i - N_i + N_i \log (N_i/M_i)]$ 

See Kaastra (2017)



# **Evolutionary Algorithms**





Based on the principles of natural selection.

#### **Gradient-free:**

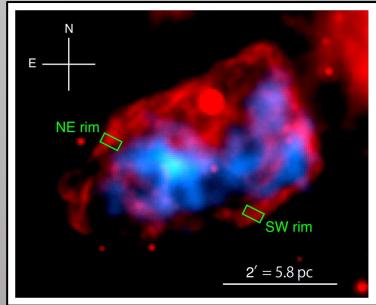
- Weak dependence on initial conditions
- Less tendency to get stuck in local minima
- Discontinuous/non-differentiable functions

#### Multi-agent:

- Evaluation of large numbers of patterns simultaneously
- Capable of outputting families of degenerate solutions

# Case Study: G41.1-0.3 (3C 397)

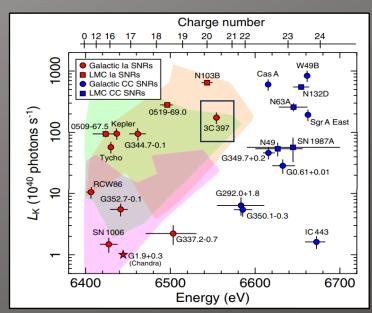
#### G41.1-0.3 Western Lobe

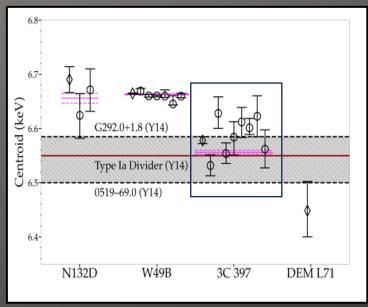


Yamaguchi et al. 2015

- Centroids dependent on position within the PWN.
- More sensitive diagnostics need to be explored.

- Type Ia SNRs tend to be significantly less ionized than CC remnants.
- Different species and ions can populate the same line intensities → degeneracy

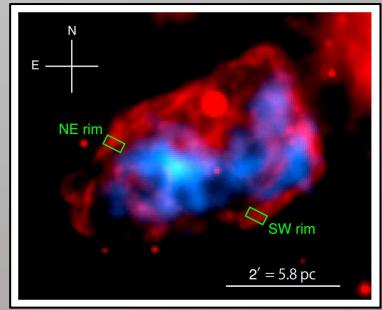




Yamaguchi et al. 2014

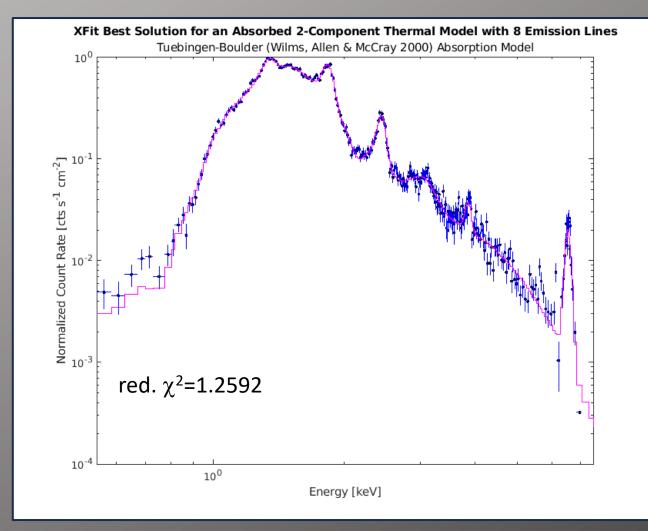
# Case Study: G41.1-0.3

#### G41.1-0.3 Western Lobe



Yamaguchi et al. 2015





Parameter

Bremss(1) 1 kT

Bremss(2) kT

Gauss(1) E0

Gauss(2) E0

Gauss(3) E0 Gauss(3) sigma

Gauss(4) E0

Gauss(5) E0

Bremss(1) Norm

Bremss(2) Norm

Gauss(1) sigma

Gauss(1) Norm

Gauss(2) sigma Gauss(2) Norm

Gauss(3) Norm

Gauss(4) sigma Gauss(4) Norm

Gauss(5) sigma

Gauss(5) Norm Gauss(6) E0

Gauss(6) sigma

Gauss(6) Norm

Gauss(7) sigma Gauss(7) Norm

Gauss(8) sigma

Gauss(7) E0

Gauss(8) E0

Gauss(8)

Value

6.2980

0.15892

505.13

2.0499

0.00271

0.52783

0.15241

647.64

1.3348 0.00138

0.00945

1.8269

0.02761

0.00095 2.2890

0.19262

0.00041

2.4309

0.00388

0.00018

2.9587

0.20612

0.00011

3.8497 0.00399

9.55e-06

6.5465

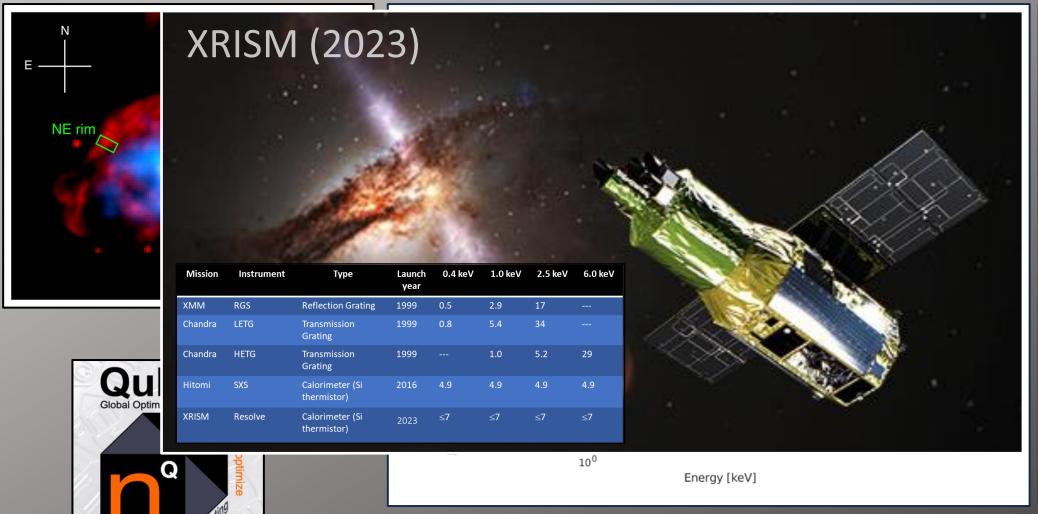
0.06932

4.28e-05

See: Rogers.	A., Safi-Harb	. S., and Fiege, J.	(2015)	for more information	n on <b>XFi</b> t

# Case Study: G41.1-0.3

## G41.1-0.3 Western Lobe



nH         6.2980           Bremss(1) 1 kT         0.15892           Bremss(1) Norm         505.13           Bremss(2) kT         2.0499           Bremss(2) Norm         0.00271           Gauss(1) E0         0.52783           Gauss(1) sigma         0.15241           Gauss(2) E0         1.3348           Gauss(2) sigma         0.00138           Gauss(2) Norm         0.00945           Gauss(3) E0         1.8269           Gauss(3) sigma         0.02761           Gauss(3) Norm         0.00095           Gauss(4) E0         2.2890           Gauss(4) sigma         0.19262           Gauss(4) Norm         0.00041           Gauss(5) sigma         0.00388           Gauss(5) Norm         0.00018           Gauss(6) E0         2.9587           Gauss(6) Sigma         0.20612           Gauss(7) Norm         0.00399           Gauss(7) Norm         9.55e-06           Gauss(8) E0         6.5465           Gauss(8) sigma         0.06932           Gauss(8)         4.28e-05	Parameter	Value	
Bremss(1) Norm         505.13           Bremss(2) kT         2.0499           Bremss(2) Norm         0.00271           Gauss(1) E0         0.52783           Gauss(1) sigma         0.15241           Gauss(1) Norm         647.64           Gauss(2) E0         1.3348           Gauss(2) sigma         0.00138           Gauss(2) Norm         0.00945           Gauss(3) Sigma         0.02761           Gauss(3) Norm         0.00095           Gauss(4) E0         2.2890           Gauss(4) sigma         0.19262           Gauss(4) Norm         0.00041           Gauss(5) E0         2.4309           Gauss(5) sigma         0.00388           Gauss(5) Norm         0.00018           Gauss(6) sigma         0.20612           Gauss(6) sigma         0.20612           Gauss(7) E0         3.8497           Gauss(7) sigma         0.00399           Gauss(8) E0         6.5465           Gauss(8) sigma         0.06932	nH	6.2980	
Bremss(2) kT         2.0499           Bremss(2) Norm         0.00271           Gauss(1) E0         0.52783           Gauss(1) sigma         0.15241           Gauss(1) Norm         647.64           Gauss(2) E0         1.3348           Gauss(2) sigma         0.00138           Gauss(3) E0         1.8269           Gauss(3) sigma         0.02761           Gauss(3) Norm         0.00095           Gauss(4) E0         2.2890           Gauss(4) sigma         0.19262           Gauss(4) Norm         0.00041           Gauss(5) sigma         0.00388           Gauss(5) Norm         0.00018           Gauss(6) E0         2.9587           Gauss(6) sigma         0.20612           Gauss(6) Norm         0.00011           Gauss(7) sigma         0.00399           Gauss(8) E0         6.5465           Gauss(8) sigma         0.06932	Bremss(1) 1 kT	0.15892	
Bremss(2) Norm         0.00271           Gauss(1) E0         0.52783           Gauss(1) sigma         0.15241           Gauss(1) Norm         647.64           Gauss(2) E0         1.3348           Gauss(2) sigma         0.00138           Gauss(2) Norm         0.00945           Gauss(3) E0         1.8269           Gauss(3) sigma         0.02761           Gauss(3) Norm         0.00095           Gauss(4) E0         2.2890           Gauss(4) sigma         0.19262           Gauss(4) Norm         0.00041           Gauss(5) sigma         0.00388           Gauss(5) Norm         0.00018           Gauss(6) E0         2.9587           Gauss(6) sigma         0.20612           Gauss(7) Norm         0.00399           Gauss(7) Norm         9.55e-06           Gauss(8) E0         6.5465           Gauss(8) sigma         0.06932	Bremss(1) Norm	505.13	
Gauss(1) E0         0.52783           Gauss(1) sigma         0.15241           Gauss(2) E0         1.3348           Gauss(2) sigma         0.00138           Gauss(2) Norm         0.00945           Gauss(3) E0         1.8269           Gauss(3) sigma         0.02761           Gauss(3) Norm         0.00095           Gauss(4) E0         2.2890           Gauss(4) sigma         0.19262           Gauss(4) Norm         0.00041           Gauss(5) E0         2.4309           Gauss(5) sigma         0.00388           Gauss(5) Norm         0.00018           Gauss(6) E0         2.9587           Gauss(6) sigma         0.20612           Gauss(7) Norm         0.0039           Gauss(7) sigma         0.00399           Gauss(8) E0         6.5465           Gauss(8) sigma         0.06932	Bremss(2) kT	2.0499	
Gauss (1) sigma         0.15241           Gauss (2) E0         1.3348           Gauss (2) sigma         0.00138           Gauss (2) Norm         0.00945           Gauss (3) E0         1.8269           Gauss (3) sigma         0.02761           Gauss (3) Norm         0.00095           Gauss (4) E0         2.2890           Gauss (4) sigma         0.19262           Gauss (5) E0         2.4309           Gauss (5) sigma         0.00388           Gauss (5) Norm         0.00018           Gauss (6) sigma         0.20612           Gauss (6) Norm         0.00011           Gauss (7) E0         3.8497           Gauss (7) sigma         0.00399           Gauss (8) E0         6.5465           Gauss (8) sigma         0.06932	Bremss(2) Norm	0.00271	
Gauss (1) Norm         647.64           Gauss (2) E0         1.3348           Gauss (2) sigma         0.00138           Gauss (2) Norm         0.00945           Gauss (3) E0         1.8269           Gauss (3) sigma         0.02761           Gauss (3) Norm         0.00095           Gauss (4) E0         2.2890           Gauss (4) sigma         0.19262           Gauss (5) E0         2.4309           Gauss (5) sigma         0.00388           Gauss (5) Norm         0.00018           Gauss (6) sigma         0.20612           Gauss (6) Norm         0.00011           Gauss (7) E0         3.8497           Gauss (7) sigma         0.00399           Gauss (8) E0         6.5465           Gauss (8) sigma         0.06932	Gauss(1) E0	0.52783	
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Gauss(2) Norm       0.00945         Gauss(3) E0       1.8269         Gauss(3) sigma       0.02761         Gauss(3) Norm       0.00095         Gauss(4) E0       2.2890         Gauss(4) sigma       0.19262         Gauss(4) Norm       0.00041         Gauss(5) E0       2.4309         Gauss(5) sigma       0.00388         Gauss(6) E0       2.9587         Gauss(6) sigma       0.20612         Gauss(6) Norm       0.00011         Gauss(7) E0       3.8497         Gauss(7) sigma       0.00399         Gauss(8) E0       6.5465         Gauss(8) sigma       0.06932	Gauss(2) E0	1.3348	
Gauss(3)       E0       1.8269         Gauss(3)       sigma       0.02761         Gauss(3)       Norm       0.00095         Gauss(4)       E0       2.2890         Gauss(4)       sigma       0.19262         Gauss(4)       Norm       0.00041         Gauss(5)       E0       2.4309         Gauss(5)       sigma       0.00388         Gauss(5)       Norm       0.00018         Gauss(6)       E0       2.9587         Gauss(6)       sigma       0.20612         Gauss(6)       Norm       0.00011         Gauss(7)       E0       3.8497         Gauss(7)       sigma       0.00399         Gauss(8)       E0       6.5465         Gauss(8)       sigma       0.06932	Gauss(2) sigma	0.00138	
Gauss(3) sigma       0.02761         Gauss(3) Norm       0.00095         Gauss(4) E0       2.2890         Gauss(4) sigma       0.19262         Gauss(4) Norm       0.00041         Gauss(5) E0       2.4309         Gauss(5) sigma       0.00388         Gauss(5) Norm       0.00018         Gauss(6) E0       2.9587         Gauss(6) sigma       0.20612         Gauss(6) Norm       0.00011         Gauss(7) E0       3.8497         Gauss(7) sigma       0.00399         Gauss(8) E0       6.5465         Gauss(8) sigma       0.06932	Gauss(2) Norm	0.00945	
Gauss (3)       Norm       0.00095         Gauss (4)       E0       2.2890         Gauss (4)       sigma       0.19262         Gauss (4)       Norm       0.00041         Gauss (5)       E0       2.4309         Gauss (5)       sigma       0.00388         Gauss (5)       Norm       0.00018         Gauss (6)       E0       2.9587         Gauss (6)       sigma       0.20612         Gauss (6)       Norm       0.00011         Gauss (7)       E0       3.8497         Gauss (7)       sigma       0.00399         Gauss (8)       E0       6.5465         Gauss (8)       sigma       0.06932	Gauss(3) E0	1.8269	
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Gauss (5)       E0       2.4309         Gauss (5)       sigma       0.00388         Gauss (5)       Norm       0.00018         Gauss (6)       E0       2.9587         Gauss (6)       sigma       0.20612         Gauss (6)       Norm       0.00011         Gauss (7)       E0       3.8497         Gauss (7)       sigma       0.00399         Gauss (8)       E0       6.5465         Gauss (8)       sigma       0.06932	Gauss(4) sigma	0.19262	
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Gauss (6)       E0       2.9587         Gauss (6)       sigma       0.20612         Gauss (6)       Norm       0.00011         Gauss (7)       E0       3.8497         Gauss (7)       sigma       0.00399         Gauss (7)       Norm       9.55e-06         Gauss (8)       E0       6.5465         Gauss (8)       sigma       0.06932	Gauss(5) sigma	0.00388	
Gauss (6) sigma       0.20612         Gauss (6) Norm       0.00011         Gauss (7) E0       3.8497         Gauss (7) sigma       0.00399         Gauss (7) Norm       9.55e-06         Gauss (8) E0       6.5465         Gauss (8) sigma       0.06932	Gauss(5) Norm	0.00018	
Gauss (6)       Norm       0.00011         Gauss (7)       E0       3.8497         Gauss (7)       sigma       0.00399         Gauss (7)       Norm       9.55e-06         Gauss (8)       E0       6.5465         Gauss (8)       sigma       0.06932	Gauss(6) E0	2.9587	
Gauss (7) E0       3.8497         Gauss (7) sigma       0.00399         Gauss (7) Norm       9.55e-06         Gauss (8) E0       6.5465         Gauss (8) sigma       0.06932	Gauss(6) sigma	0.20612	
Gauss (7) sigma       0.00399         Gauss (7) Norm       9.55e-06         Gauss (8) E0       6.5465         Gauss (8) sigma       0.06932	Gauss(6) Norm	0.00011	
Gauss (7) Norm 9.55e-06 Gauss (8) E0 6.5465 Gauss (8) sigma 0.06932	Gauss(7) E0	3.8497	
Gauss(8) E0 6.5465 Gauss(8) sigma 0.06932	Gauss(7) sigma	0.00399	
Gauss(8) sigma   0.06932	Gauss(7) Norm	9.55e-06	
( ) 0	Gauss(8) E0	6.5465	
Gauss(8) 4.28e-05	Gauss(8) sigma	0.06932	
(-)	Gauss(8)	4.28e-05	

See: Rogers, A., Safi-Harb, S., and Fiege, J. (2015) for more information on XFit

# References

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# Thank you!