

**Models of Inefficient Accretion**  
**onto a Black Hole**  
**and Pair Production in Jets**

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# Radiatively Inefficient Accretion Flows (RIAFs)

- RIAF in theory
  - $\dot{m} < \dot{m}_{\text{crit}} = \text{few} \times 10^{-7}$  ( $\dot{m} = \dot{M}_{\text{acc}} / \dot{M}_{\text{Edd}}$ ,  $\dot{M}_{\text{Edd}} = 10\% L_{\text{Edd}} / c^2$   
 $L_{\text{Edd}} = 4\pi G M_{\text{bh}} c m_p / \sigma_T$ )
  - $t_{\text{rad}} \gg t_{\text{dyn}}$ , weak radiative cooling, energy advection (ADAF, Narayan & Yi 1994)
  - Accretion flow  $\rightarrow$  geometrically thick and optically thin + accretion flow dynamics decoupled from radiation
  - collisionless plasma  $\rightarrow T_p / T_e \neq 1$
- RIAF in practice, BH systems with  $L \ll L_{\text{Edd}}$ 
  - quiescent GN: Sgr A\* ( $L / L_{\text{Edd}} = 10^{-9}$ )
  - BLLac/FRI: M87 ( $L / L_{\text{Edd}} = 10^{-5.5}$ )
  - many nearby galactic nuclei, BHB in quiescent state

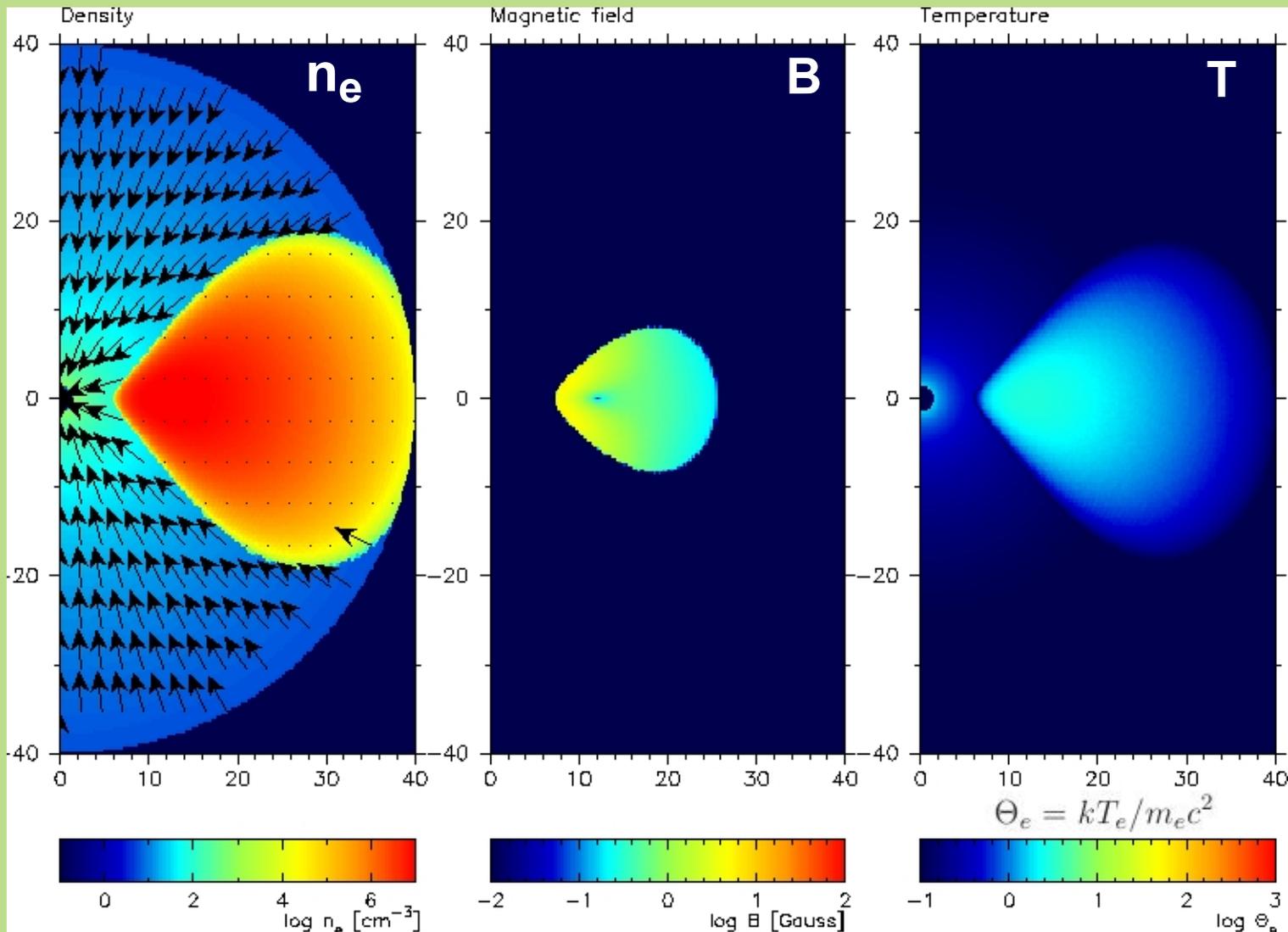
## Outline

- Numerical realization of RIAF models (GRMHD simulations)
- Radiative properties of RIAFs from Monte Carlo simulations
  - application to Sgr A\*
- Non-equilibrium electron-positron pair production in the jet (magnetized funnel)
  - $\gamma + \gamma \rightarrow e^+ + e^-$
  - pair production is balanced by pair escape rather than pair annihilation

## Goals

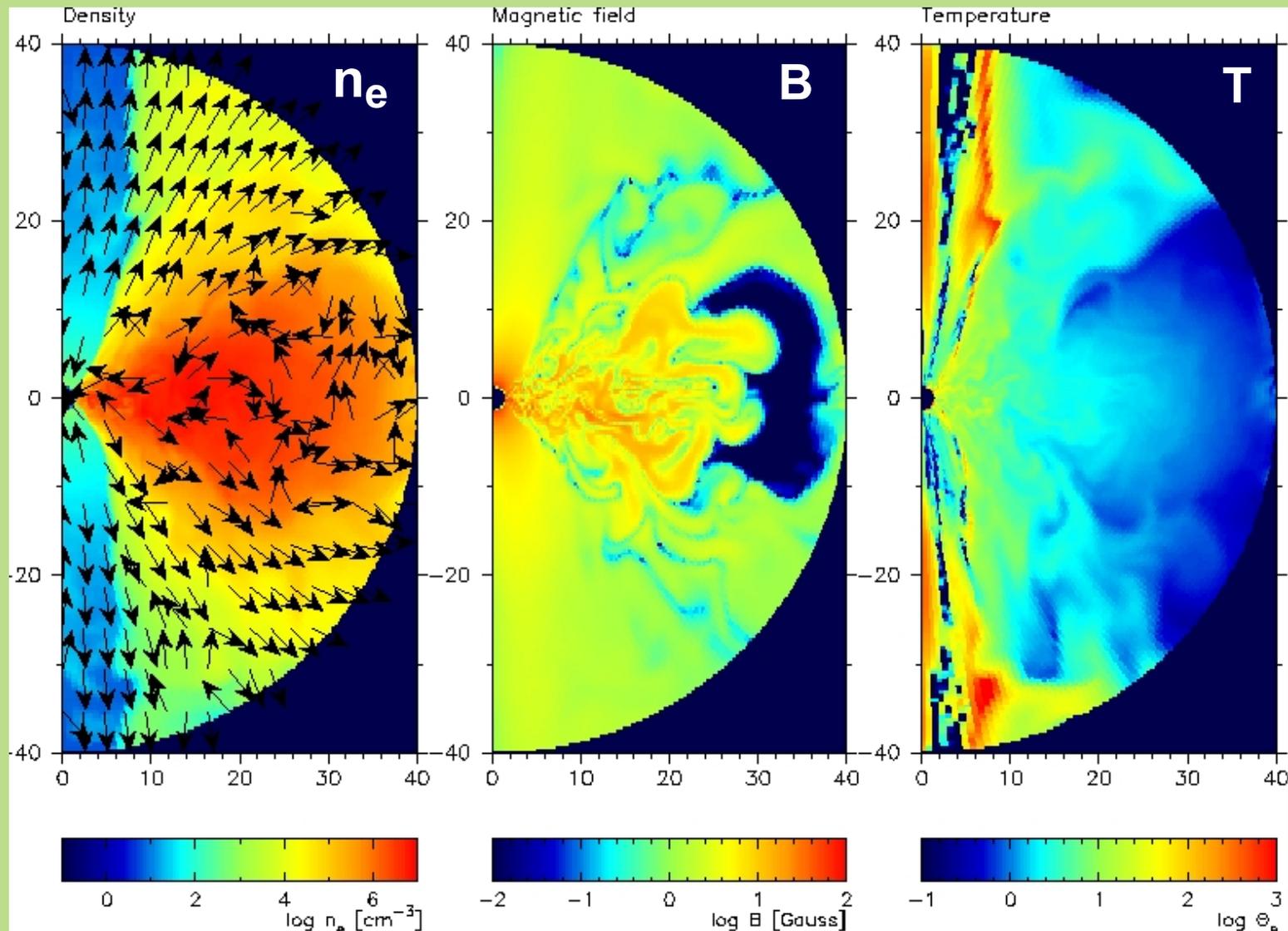
- Understand physics of accretion in underluminous X-ray sources such as Sgr A\*
- Understand composition of jets and conditions to produce jets
  - during RIAF phase
  - during transition from RIAF to efficient accretion mode
  - Selfconsistent model of accretion disk and jet

# Accretion disk model - initial setup



- Equilibrium torus (Fishbone & Moncrief 1976, Abramowicz et al. 1978) + weak magnetic field
- MHD equations solved with HARM (2D Gammie et al. 2003, 3D Noble et al. 2006, 2009), conservative, shock capturing scheme to solve GRMHD eq,
- radial range =  $r_h - 40 R_g$  (Kerr -Schild coordinates-no singularity at  $r_h$ )

# Accretion disk model - later times



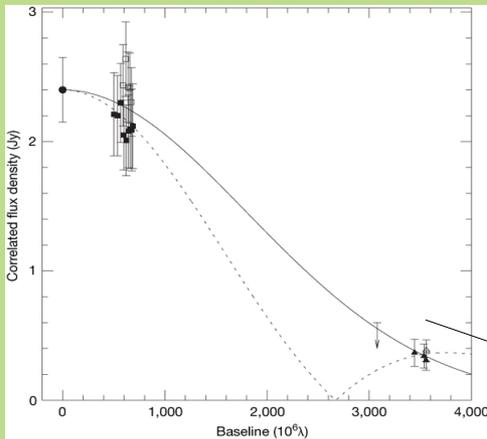
- All simulations show a similar, statistically steady final state
- We assume that the inner parts of this torus are the inner parts of large RIAF
- Scaling depends on  $M_{\text{bh}}$  and  $\dot{M}_{\text{acc}}$

# Model comparison to observation - radiative transfer

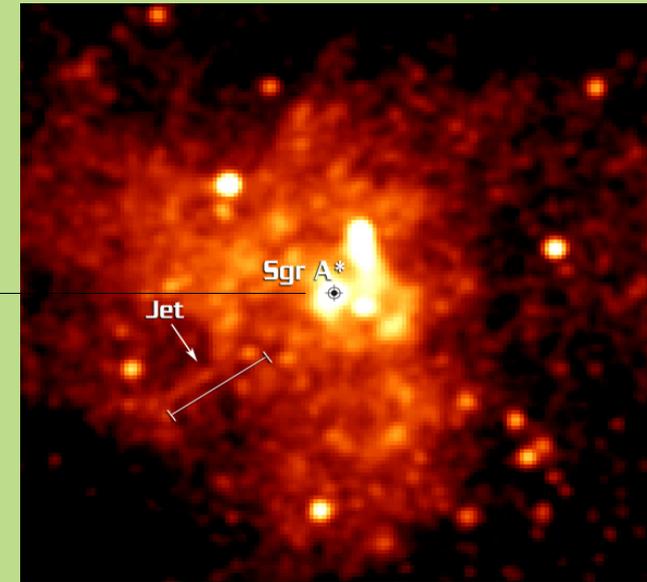
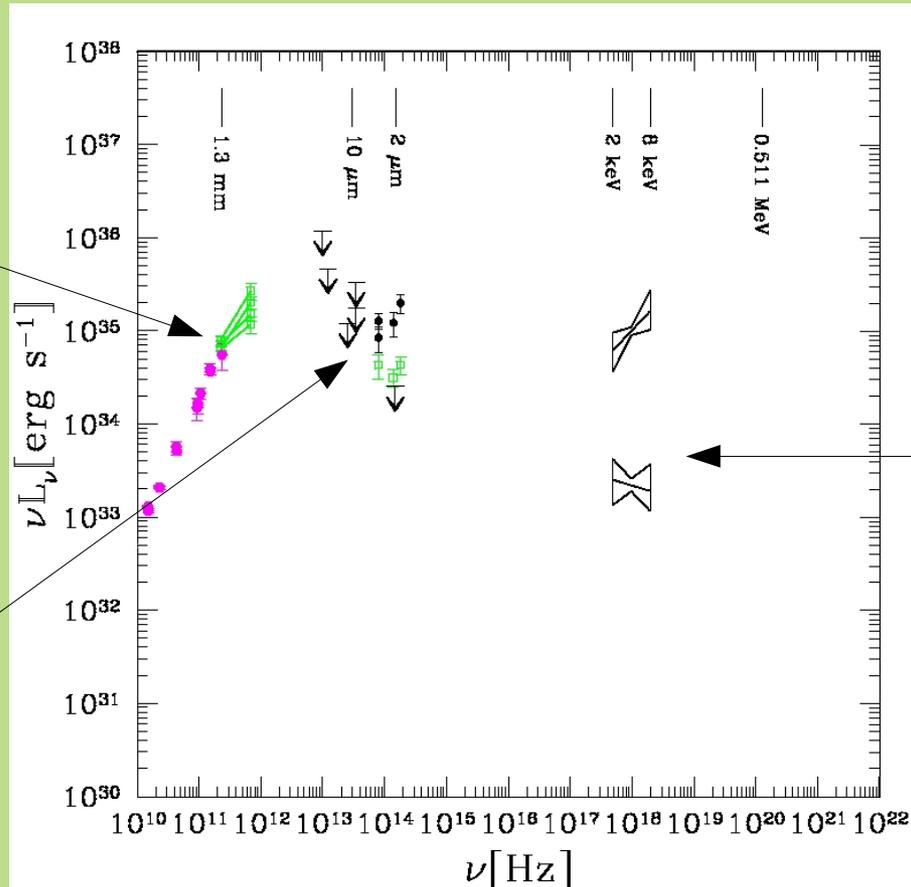
- Monte Carlo technique for radiative transfer:
  - Generate photon  $E=h\nu$  and  $\vec{p}$  based on the emissivity of the physical radiative process
  - trace individual photons to the observer
- Important emission processes in RIAF:
  - synchrotron radiation (relativistic thermal distribution of electrons)
  - Compton scattering
  - Absorption
- All relativistic effects are included: photons move on geodesics, Doppler boosting, gravitational redshift etc. (Dolence et al. 2010)

# Observations of Sgr A\* ( $M_{bh}=4 \cdot 10^6 M_{\odot}$ )

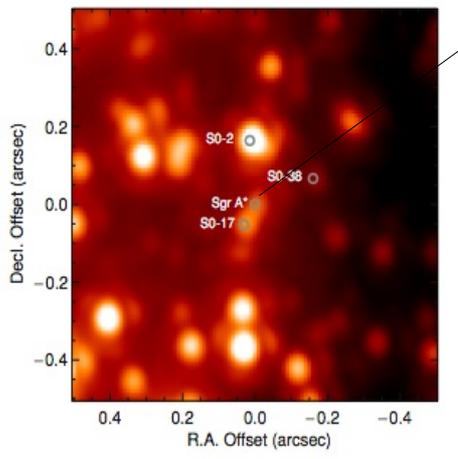
- Quiescent emission (radio, sub-mm, NIR, X-rays) + flares (NIR and X-rays)
- VLBI size of emission at 1.3 mm FWHM=37  $\mu\text{s}$ , apparent size of horizon 55  $\mu\text{s}$



VLBI, 230 GHz  
Doeleman et al.  
2009



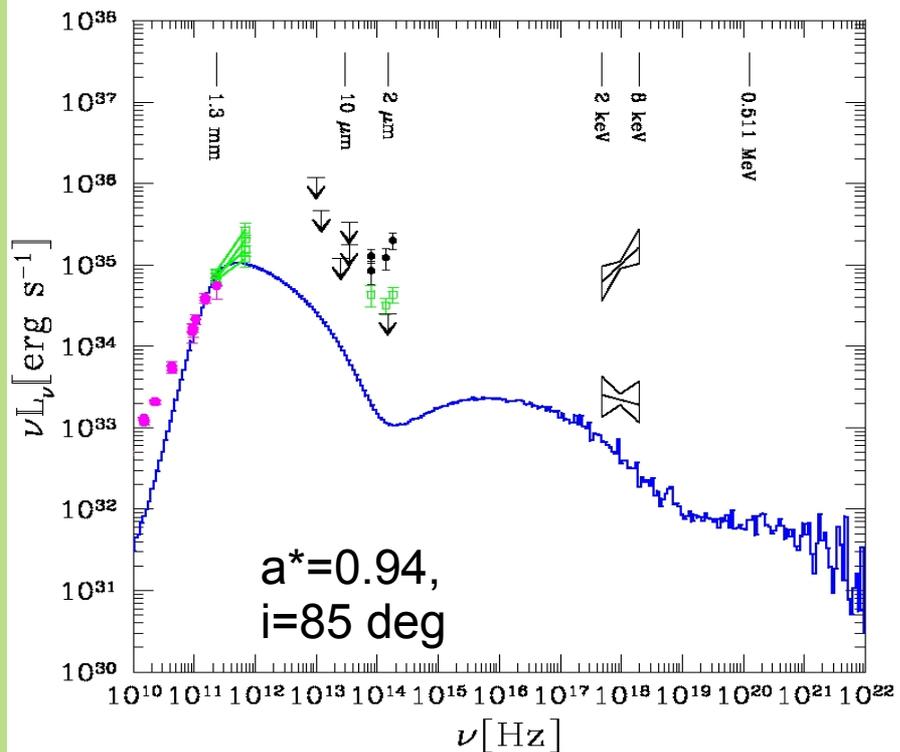
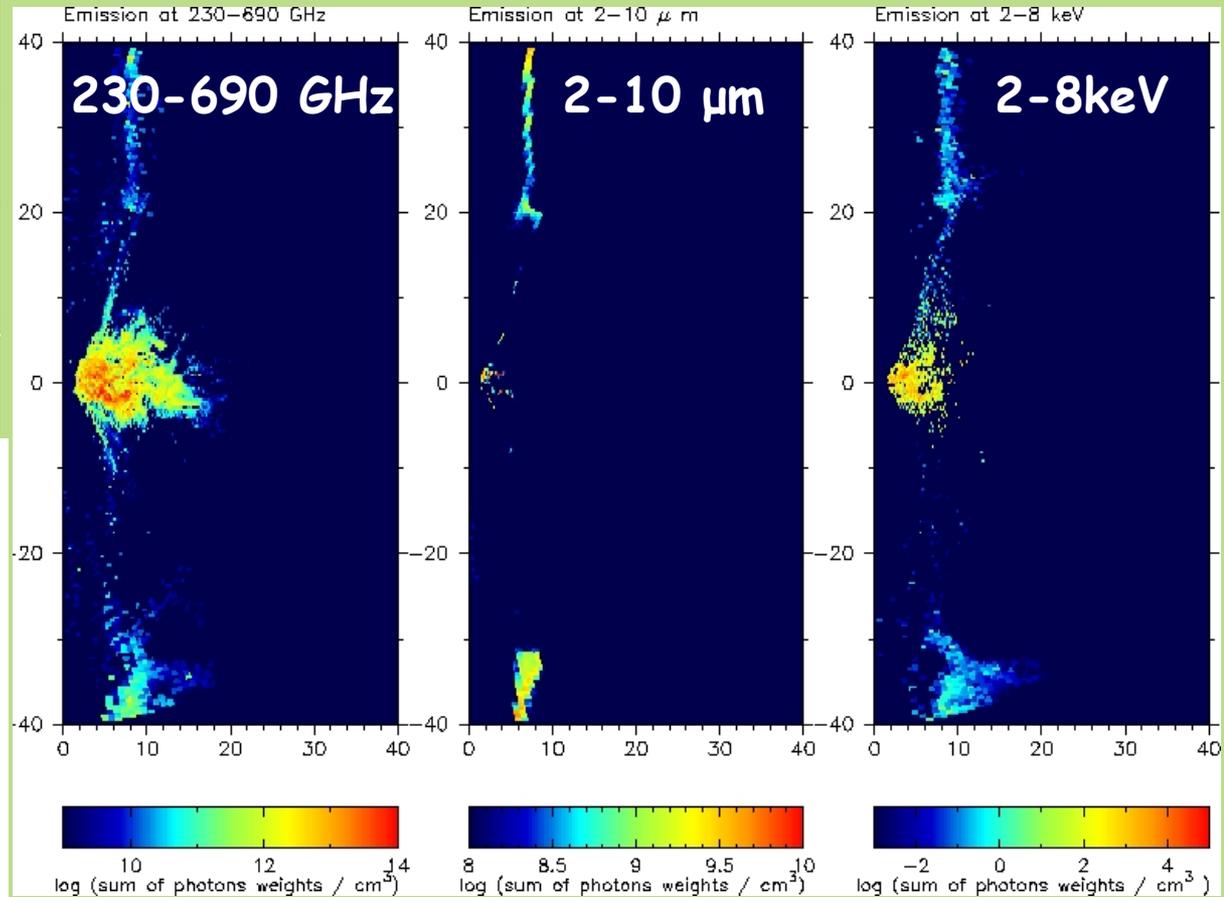
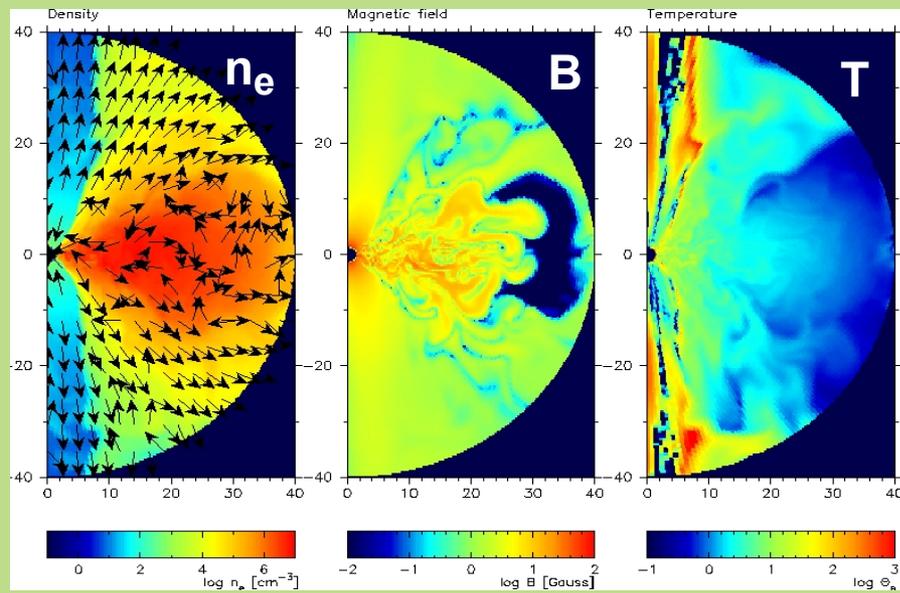
Chandra, 2-8 keV  
1.25 arcmin



Keck, NIR,  
UCLA group

- model free parameters:  $\dot{m}$ ,  $a^*$ ,  $T_p/T_e$ ,  $i$
- fit model SED to sub-mm obs., do not overproduce limits at high energies + fit the size from VLBI

# Emission from turbulent disk from Monte Carlo radiative transfer

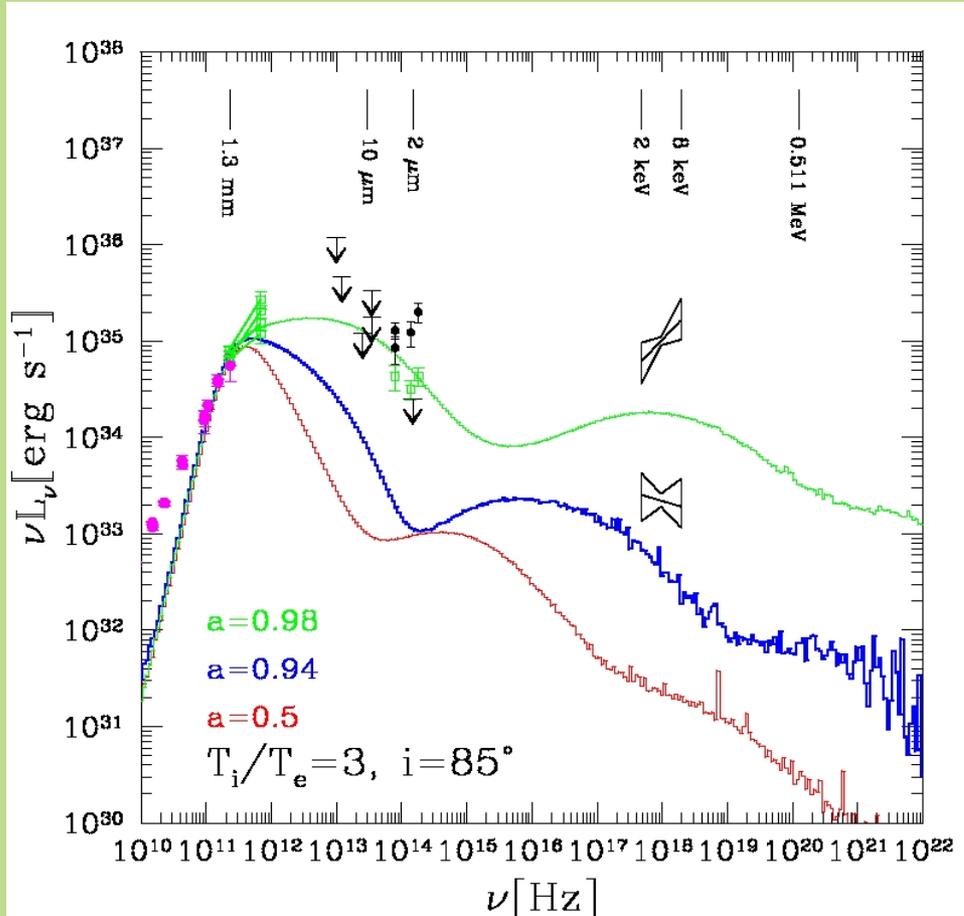


Origin of photons at different frequencies,  
Moscibrodzka et al. 2009

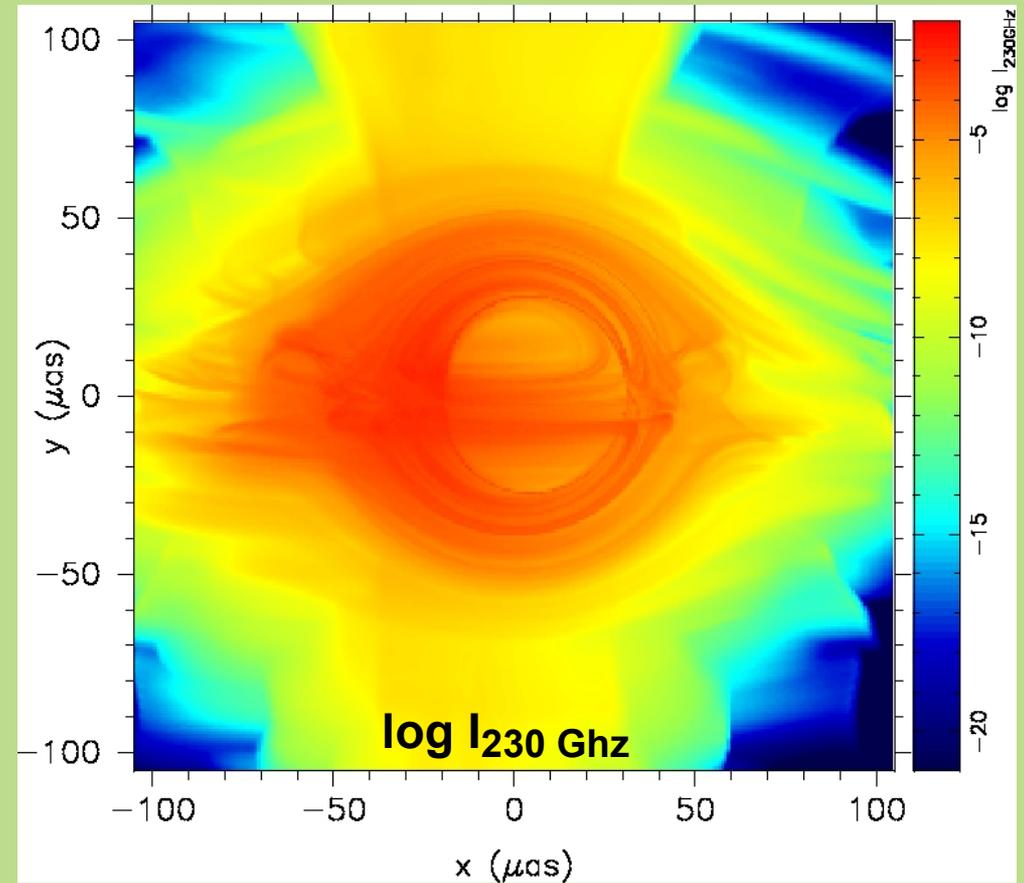
← Spectral energy distribution (SED)

# SEDs (vs. radio, NIR and X-ray)

# Images (vs. VLBI observations)



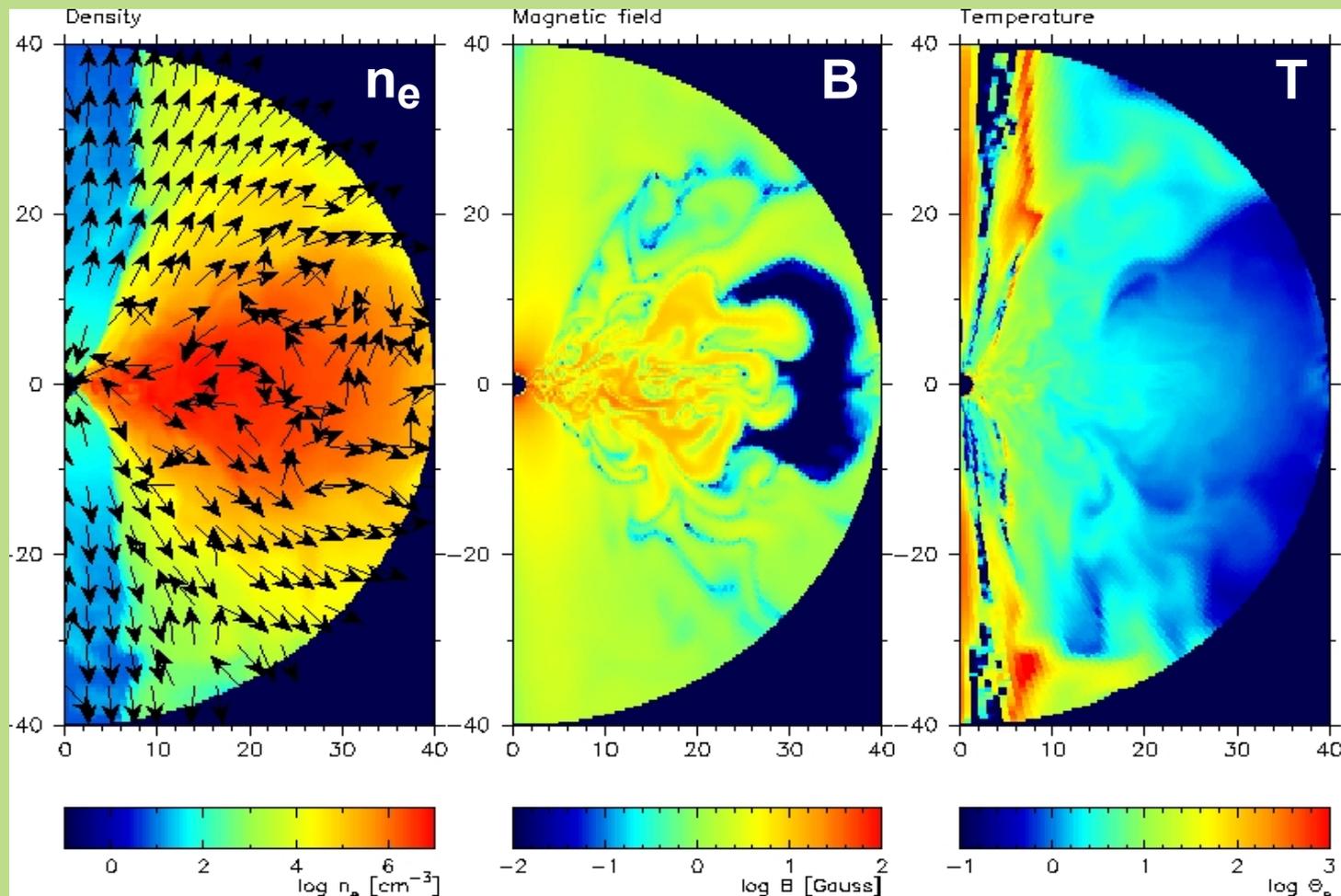
SED calculated with Monte Carlo code, Moscibrodzka et al. 2009



230 GHz image of the model (Moscibrodzka et al. 2009) calculated with ray-tracing code (Noble et al. 2007)

- 'Best-bet' model for Sgr A\* gives  $a=0.94$ ,  $T_p/T_e=3$ ,  $i \approx 90$  deg,  $\dot{m}=10^{-7}$
- $a^* < 0.94$  and  $T_p/T_e=1$  give poor fit to sub-mm observations
- $a^* > 0.94$  overestimate X-rays observations
- $T_p/T_e > 3$  wrong sub-mm slope, overestimate NIR and X-rays + produce too large images

# What are the physical conditions in the funnel ?



- In the funnel matter free to fall out
  - numerically  $\rightarrow$  floor density
- What is real density in the funnel?
- In nature funnel density in LLGN determined by  $\gamma\gamma$  pair production (Phinney 1983)
- What is the actual pair production ?

# Electron-positron jets - how many pairs do we expect?

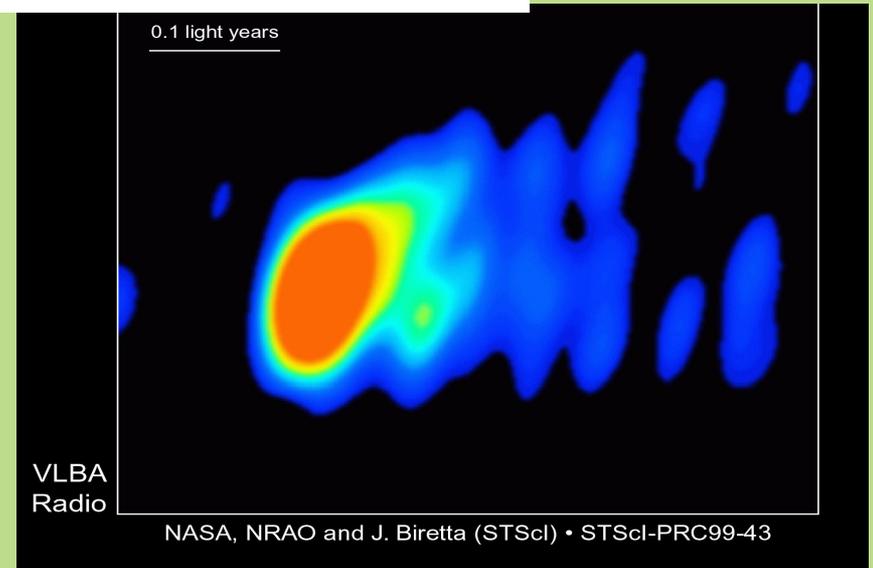
- We do not expect much of pairs to be created at all (compactness parameter, or optical depth to pair production, is small  $\tau = L\sigma_{\text{th}}/Rm_e c^3 \approx 10^{-5} \ll 1$ )

- $\dot{n}_{+/-} = n_{\gamma}^2 \sigma_{\gamma\gamma} c$ , crosssection for  $\gamma+\gamma=e^++e^-$  (Breit-Wheeler)

$$\frac{\sigma_{\gamma\gamma}}{\sigma_T} = \frac{3}{8 \epsilon_{[\text{CM}]^6}} \left[ (2 \epsilon_{[\text{CM}]^4} + 2 \epsilon_{[\text{CM}]^2} - 1) \cosh^{-1} \epsilon_{[\text{CM}]} - \epsilon_{[\text{CM}]} (\epsilon_{[\text{CM}]^2} + 1) \sqrt{\epsilon_{[\text{CM}]^2} - 1} \right]$$

- Estimate of pair plasma density
- $n_{\gamma} = L_{\gamma}/m_e c^3 R^2$ ,  $t_{\text{esc}} = R/c$ ,  $R \sim GM_{\text{bh}}/c^2$   
(pair production balanced by escape)

- Sgr A\*:  $n_{+/-} = 10^{-4} \text{ cm}^{-3}$
- M87:  $n_{+/-} = 10^4 \text{ cm}^{-3}$



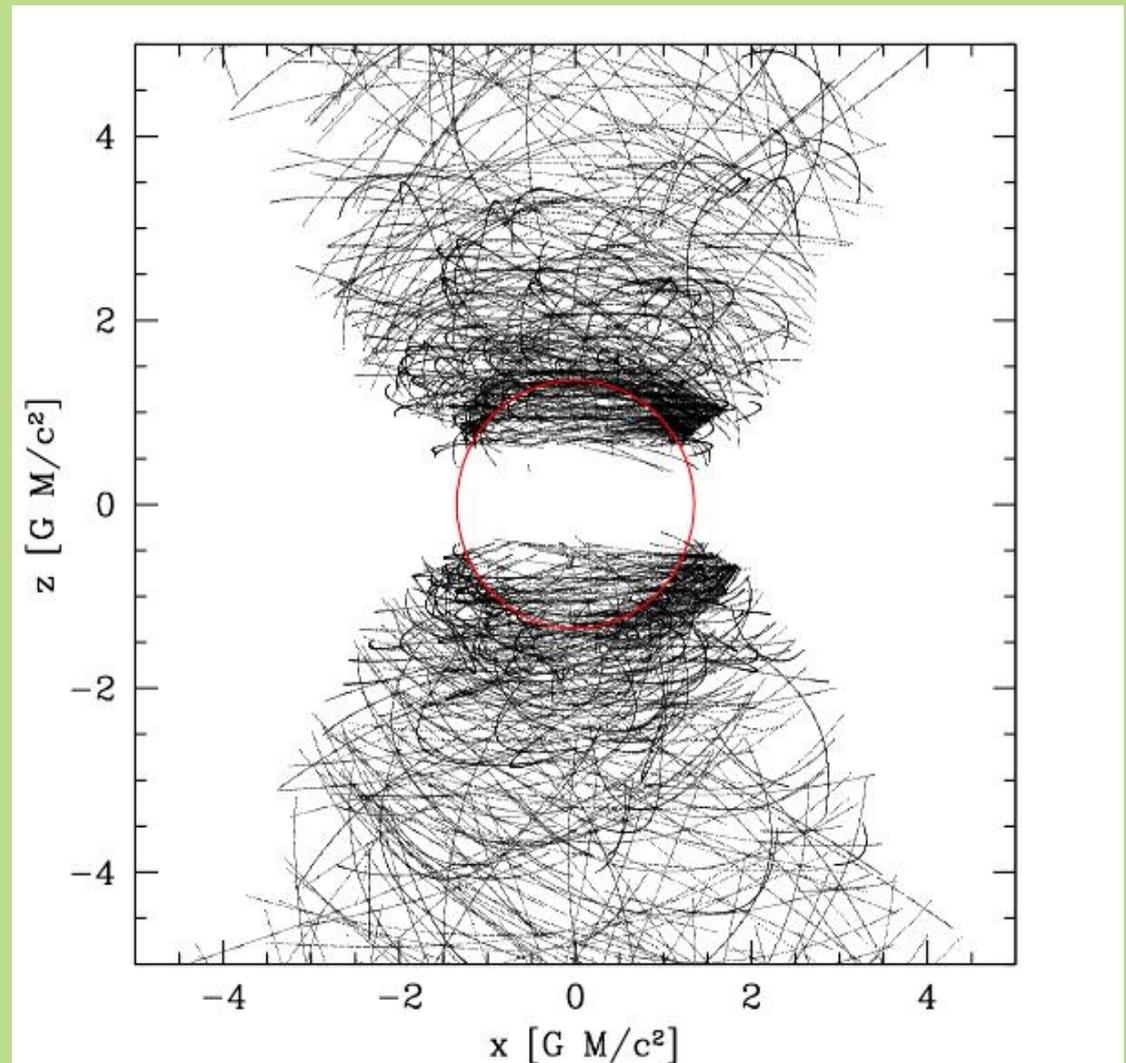
$0.1 \text{ yr} = 1000 R_g M_{\text{bh}} = 3 \cdot 10^9 M_{\odot}$ ,  $n_{+/-} = 1 \text{ cm}^{-3}$

- Problem is particularly interesting in case of M87

**With Monte Carlo radiative transfer we can do better job !**

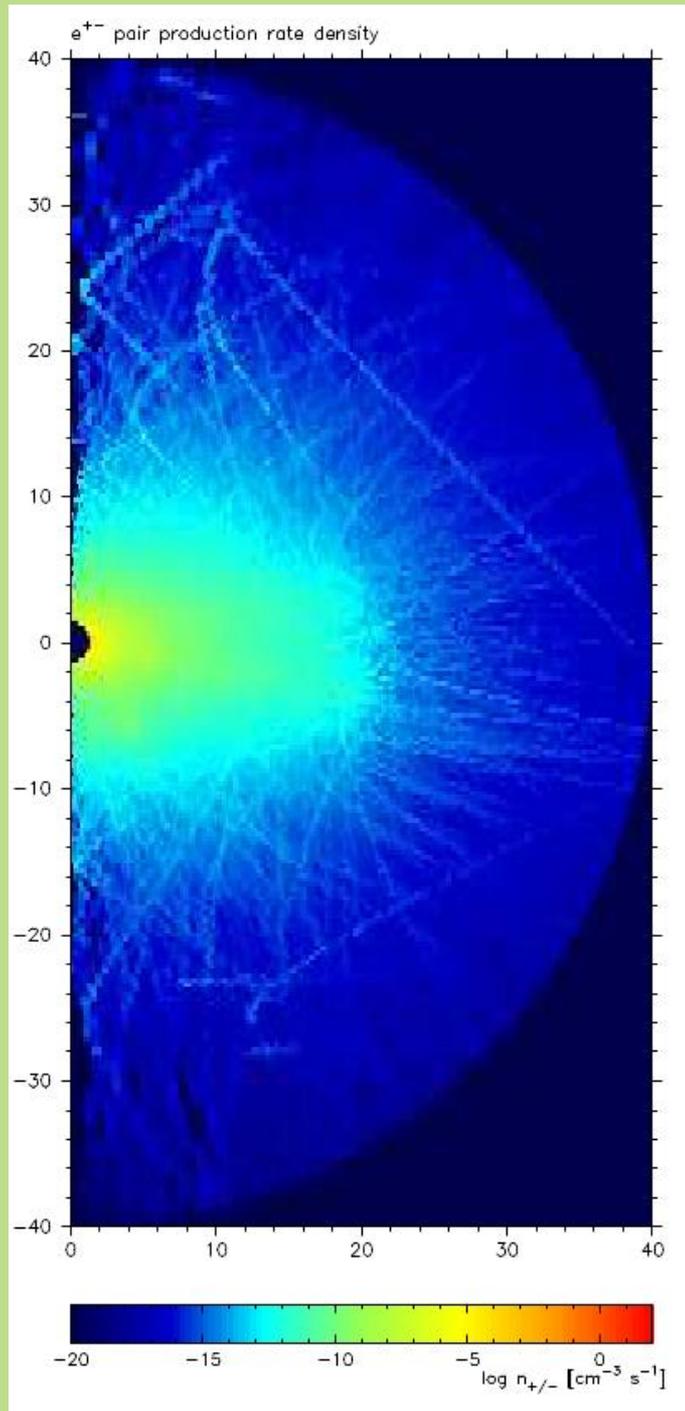
# $e^{+/-}$ pair production-Monte Carlo method

- Monte Carlo techniques allow to follow collisions between individual photons (photon packets) everywhere
- Pair production opacity assumed small
- We need to store information about the radiation field above 1 MeV (in the center-of-momentum frame)



$h\nu > 1$  MeV photon trajectories in the jet, Gammie 2009, private com.

# $e^{+/-}$ pair production rates in RIAF



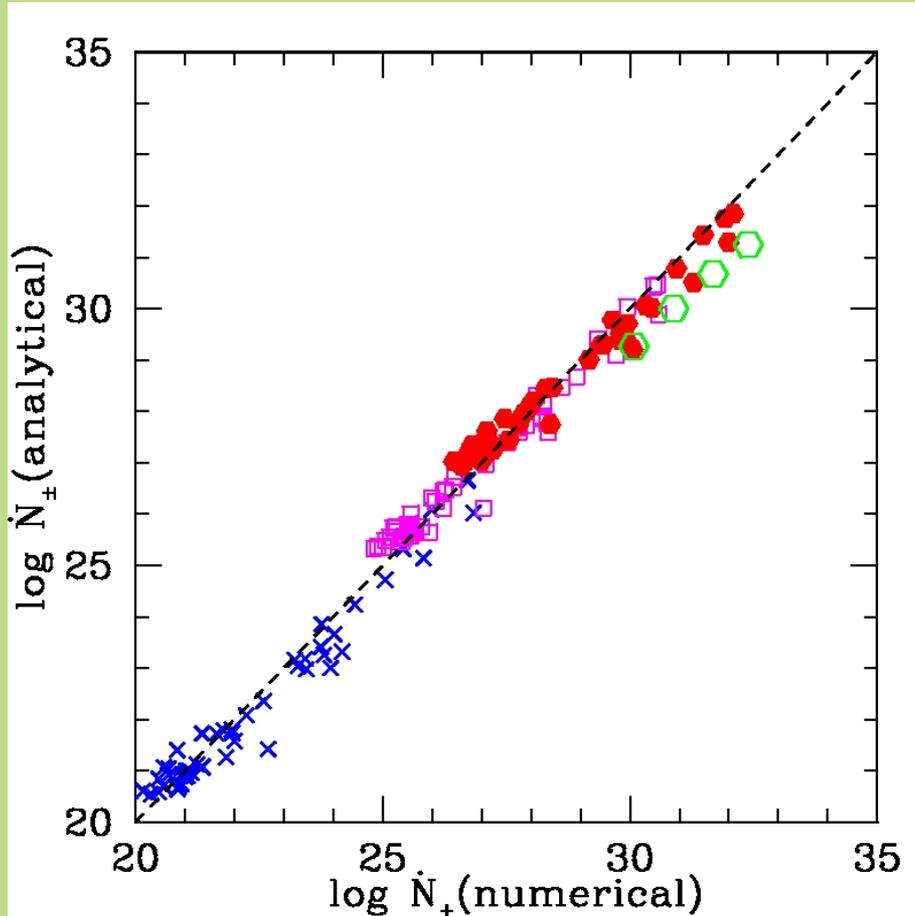
$e^{+/-}$  pair production rate !

- Disk turbulent but at a given time radiation field is smooth, pair prod. distribution is smooth
- Individual rays is Monte Carlo noise
- Beaming effects  $\rightarrow$  most of pairs created in the disk plane,  $\mu = \cos(\theta)$

$$\dot{n}_{\pm}(r, \mu) \sim r^{-6} e^{-\mu^2/0.4}$$

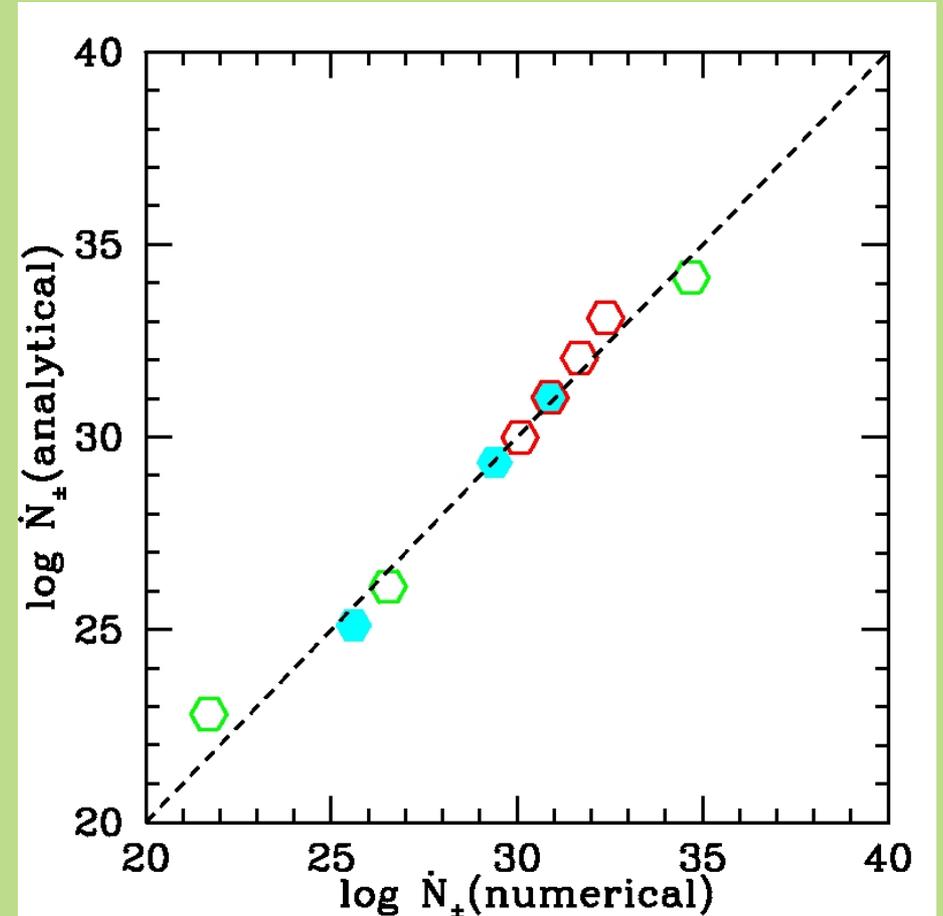
**10-20% created in the magnetically dominated funnel**

# $e^{+/-}$ pair production - dependence on observables and model parameter



Observable parameters:  $L_X$ ,  $\alpha_X$ ,  $M_{bh}$

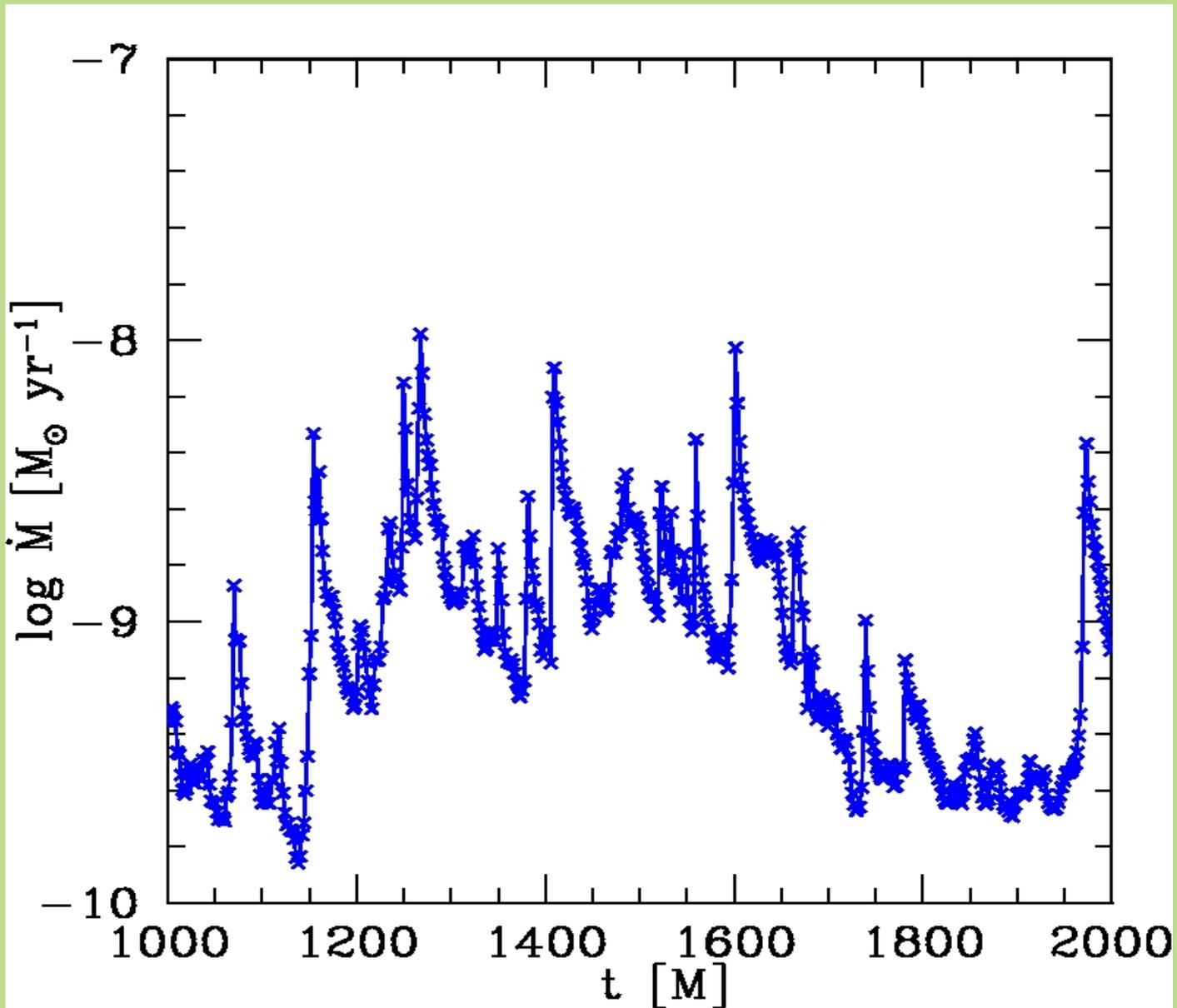
$$\dot{N}_{\pm} \sim L_X^2 e^{9.26\alpha_X} M_{BH}^{-1}$$



Model parameters:  $\dot{m}$ ,  $M_{bh}$ ,  $r_{ISCO}$

$$\dot{N}_{\pm} \sim \left(\frac{2.044}{r_{isco}}\right)^{26} \dot{m}^7 M_{BH}^2$$

# $e^{\pm}$ pair production - dependence on model parameters



Mass accretion rate vs. time at later times of simulation

## $e^{+/-}$ pair production - observational consequences

- Can we see emission from pairs? To calculate SED :
  - need pair density and distribution of pair kinetic energy
  - so need to solve dynamical equations of the pair plasma (in preparation)

### Sgr A\*

- During quiescence - small number of pairs
- During strong X-ray flare ( $L_x = 10^{35}$  ergs/s) → arising compact pair jet?
- activity in the past  $L_x = 10^{39}$  ergs/s - might have produced stronger pair jet in the past

### M87

- number of pairs slightly larger than observed one:  $n_{+/-} = 100 \text{ cm}^{-3}$
- need to couple dynamics with radiative transfer (in preparation)
- pair production suppressed by cooling

## Summary

- We model inefficient accretion onto spinning black holes using GRMHD simulations, we model multiwavelength (radio-gamma rays) radiative properties of GRMHD simulations using GR Monte Carlo techniques
- We have models of Sgr A\* quiescent emission (Moscibrodzka et al. 2009) and variability (Dolence et al. 2010, in press),  $a^*=0.94$ ,  $T_p/T_e \sim 1$ ,  $i=90^{\text{deg}}$
- For first time we compute non-equilibrium electron-positron pair production rates by  $\gamma\gamma$  from turbulent accretion disk around spinning black hole
- Production of pairs sensitive to X-ray luminosity, very sensitive to mass accretion rate and spin of the BH
- More to be done in near future !

END

# Test of pair production code

- 3D Cartesian space, 2 point sources of high energy radiation

