

Measuring the Radius of Neutron Stars

Sebastien Guillot
Robert Rutledge



Collaborators

Natalie Webb, IRAP (France)

Mathieu Servillat, CFA Harvard & CEA Saclay

*X-Ray Binaries: Celebrating 50 Years Since the Discovery of Sco-X1
Boston, MA - July 2012*

Outline

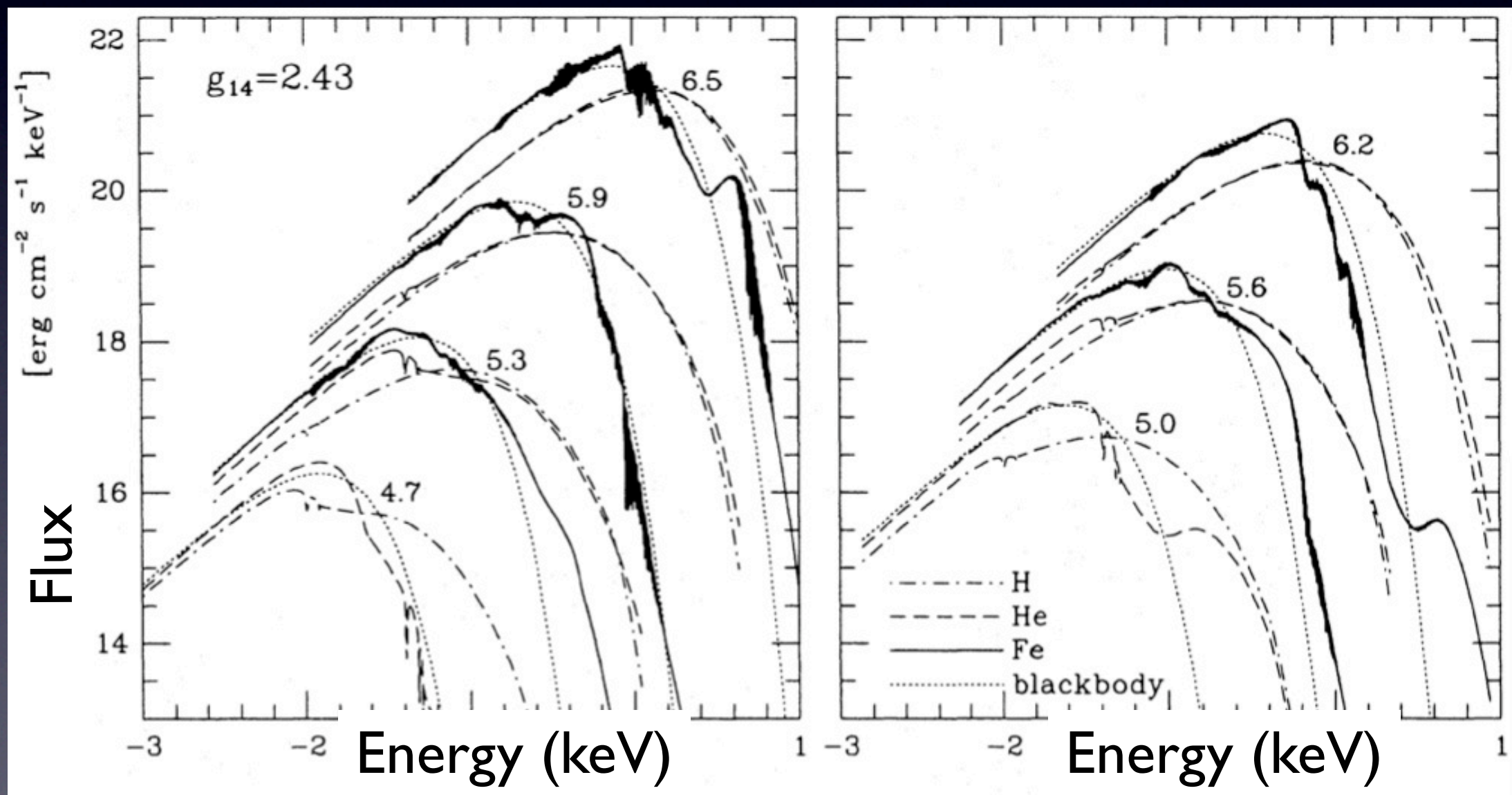
- Thermal emission of quiescent LMXBs to constrain the dense matter equation of state
- Recent measurements of masses and radii
- A new approach to measure the radius of neutron stars
- Results and constraints on the EoS

Quiescent LMXBs

- In quiescence, LMXBs have low mass accretion rate
- Thermal emission comes from the surface with $L_x = 10^{32-33}$ erg/sec
- Emission powered by deep crustal heating (Brown et al. 1998)
- Thermal emission modelled with a hydrogen atmosphere model

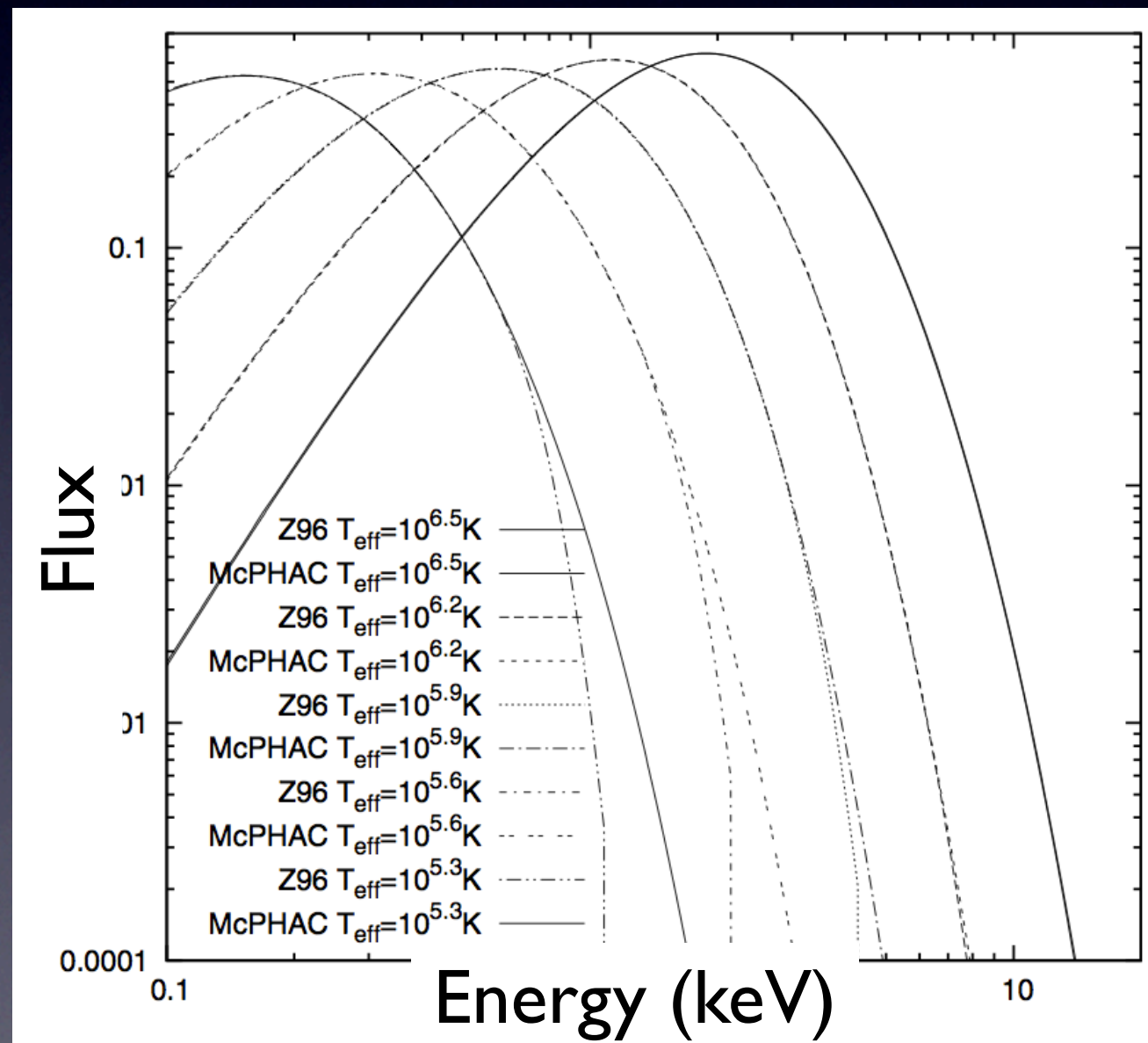
Neutron Star Hydrogen Atmosphere Models

Models by Zavlin et al. (1996), Heinke et al. (2006), Haakonsen et al. (2012)

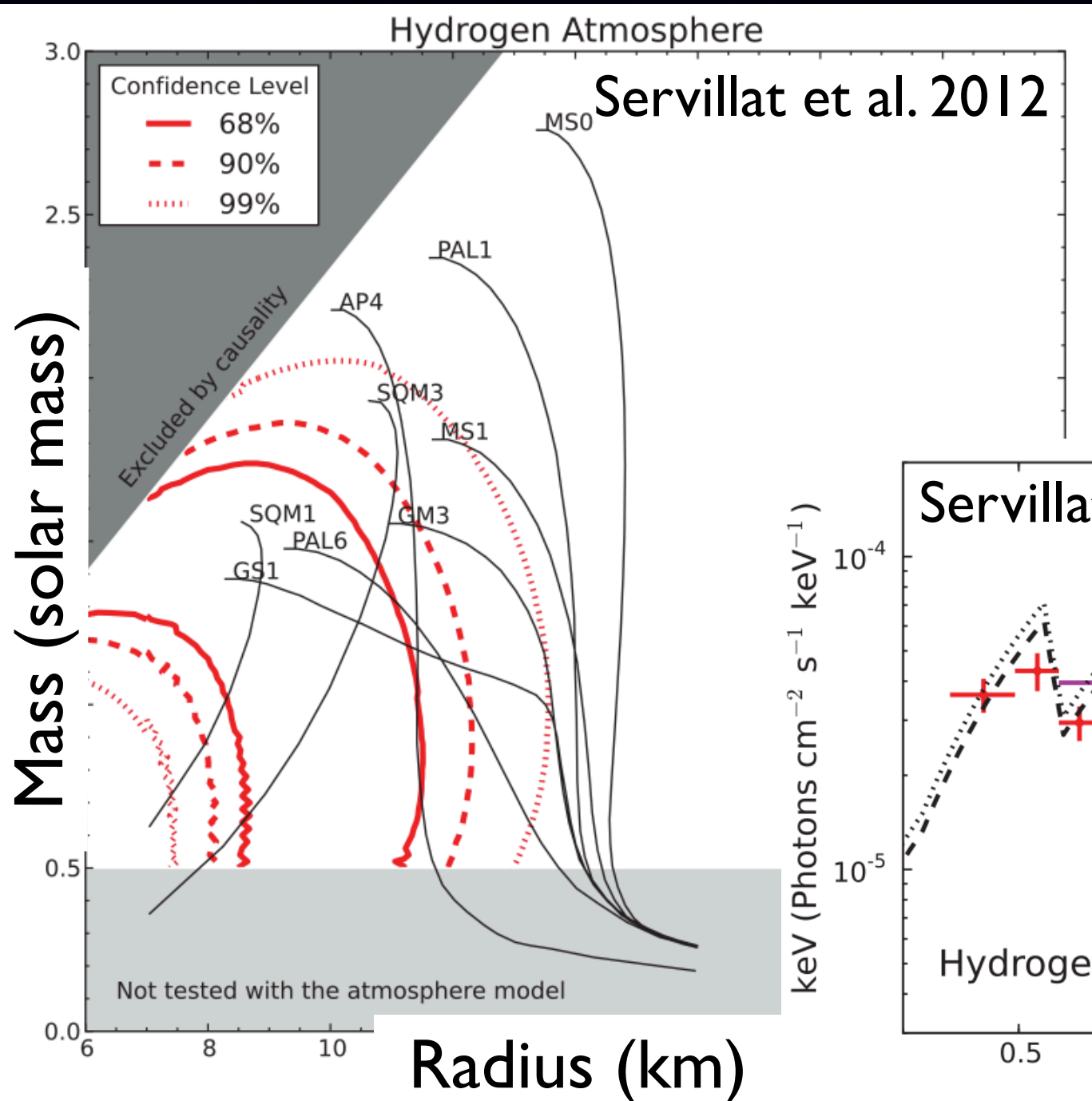


Neutron Star Hydrogen Atmosphere Models

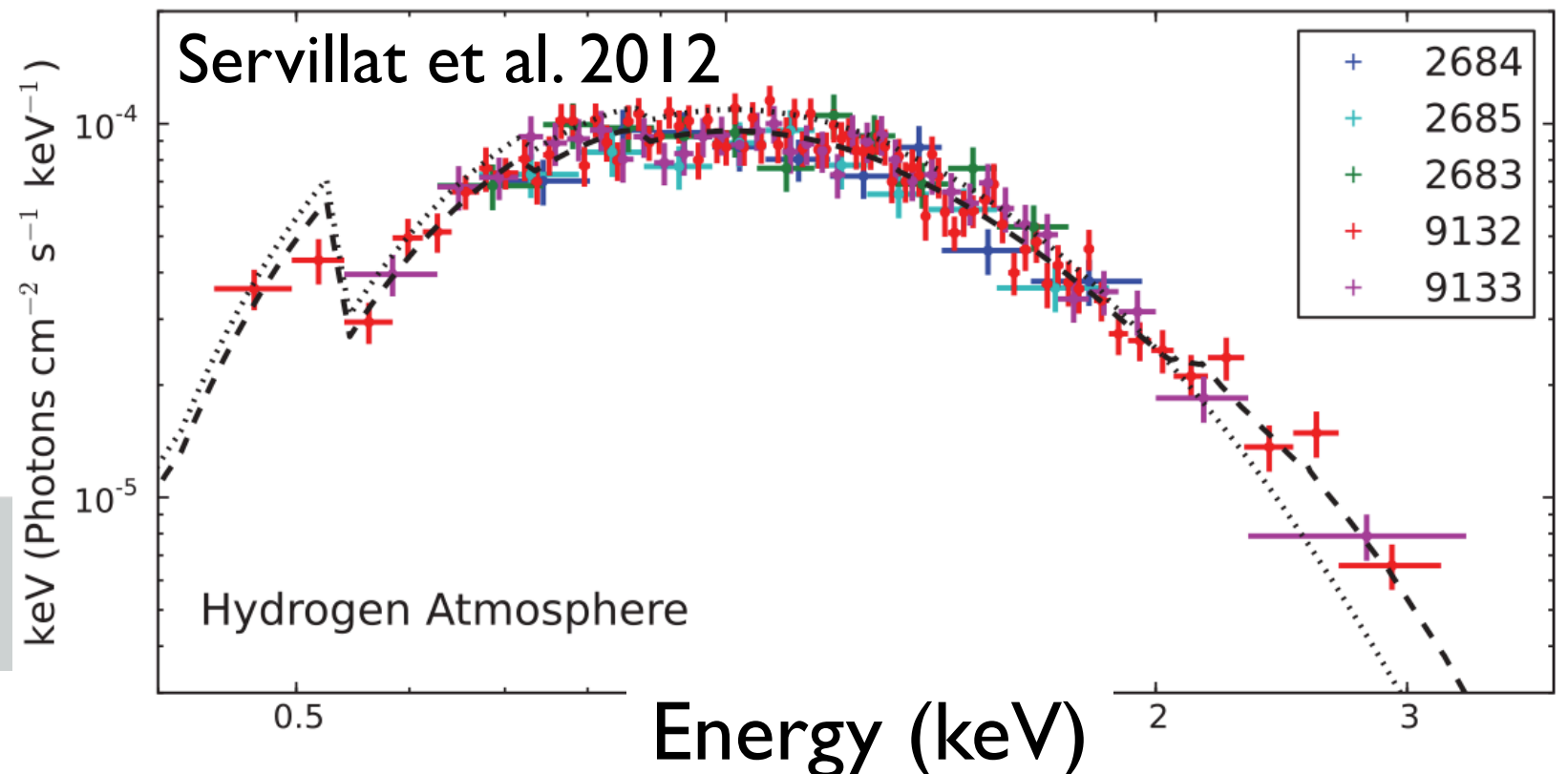
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X-Ray spectral analysis of qLMXBs



NSATMOS H-atmosphere model fits for kT_{eff} , M_{NS} , and R_{NS} , for a given distance



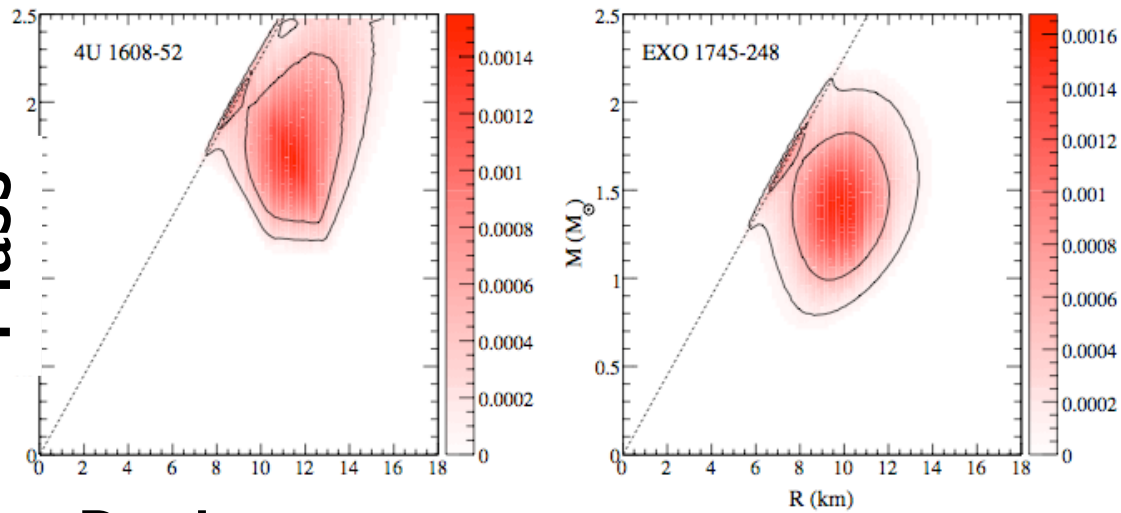
Empirical Equation of State

Steiner et al. 2010, 2012

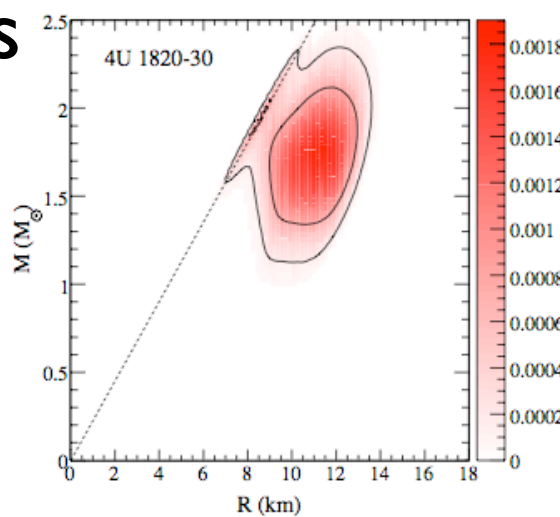
Type I X-ray bursts

Quiescent LMXBs

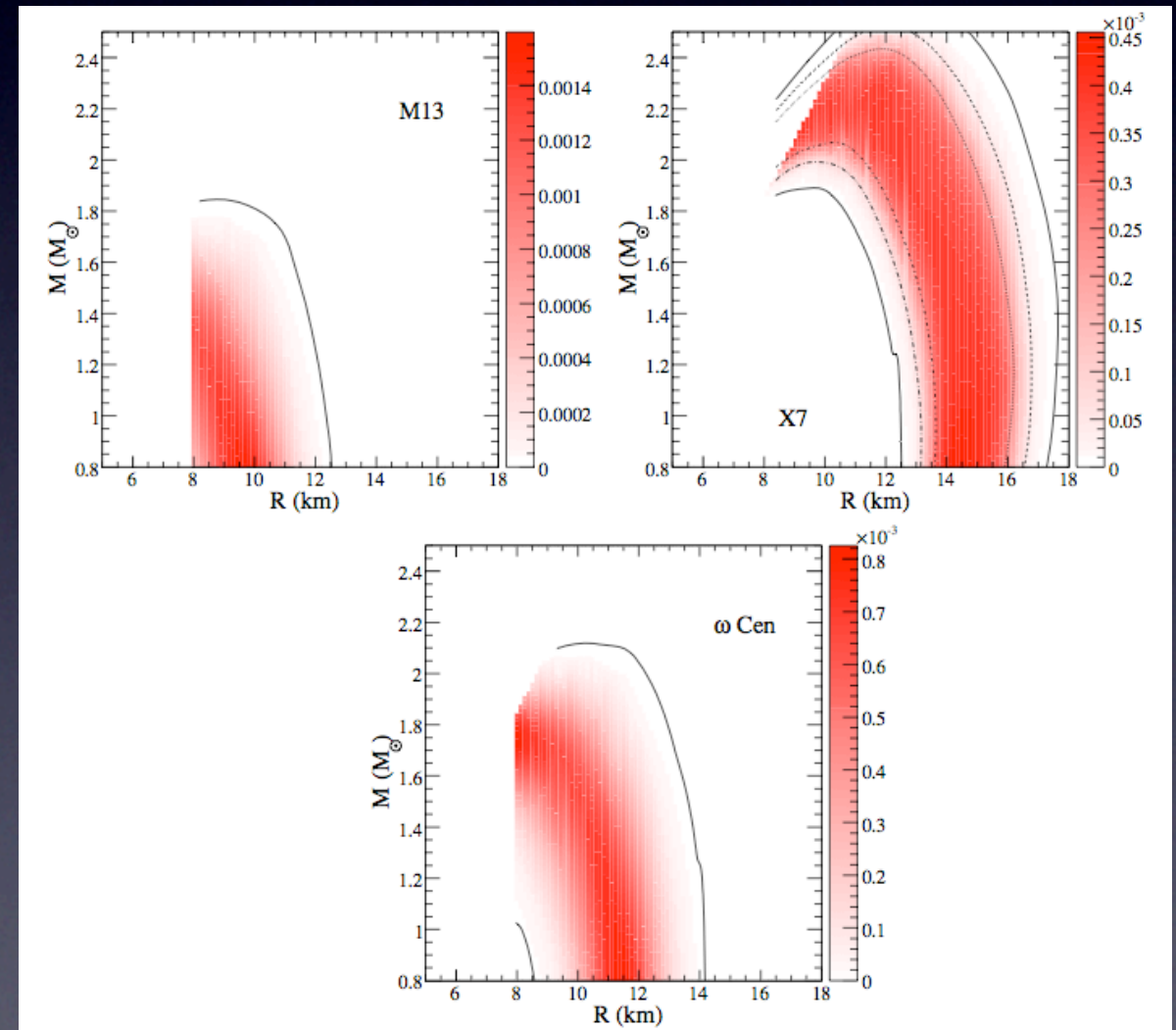
Mass



Radius



+

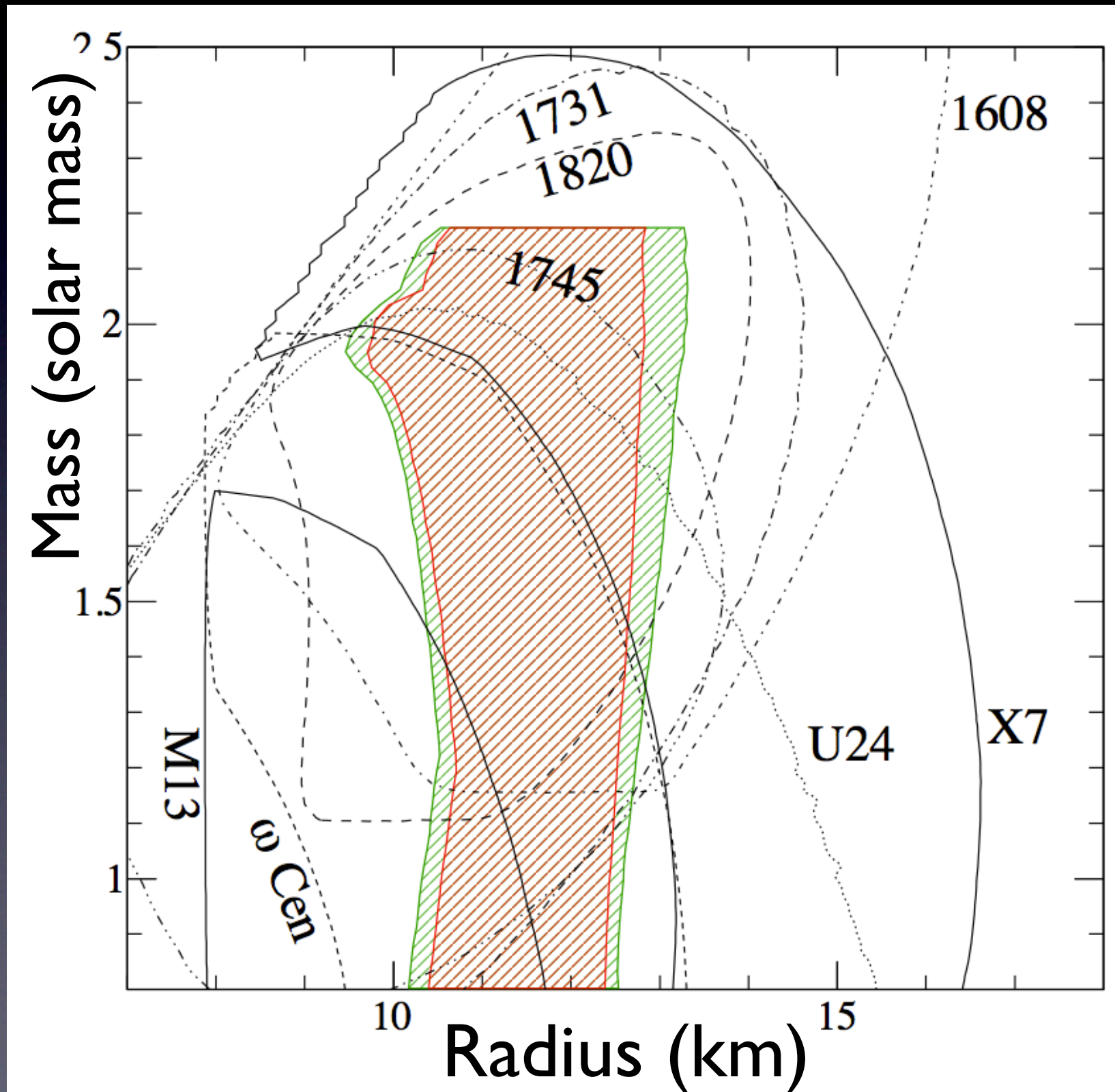


+ M-R contour of Xray burst KSI731-260
Özel et al. 2011

+ M-R contour of qLMXB in NGC6397
from Guillot et al. 2011

Empirical Equation of State

R_{NS} is roughly constrained between 10 and 13 km for a wide range of masses.

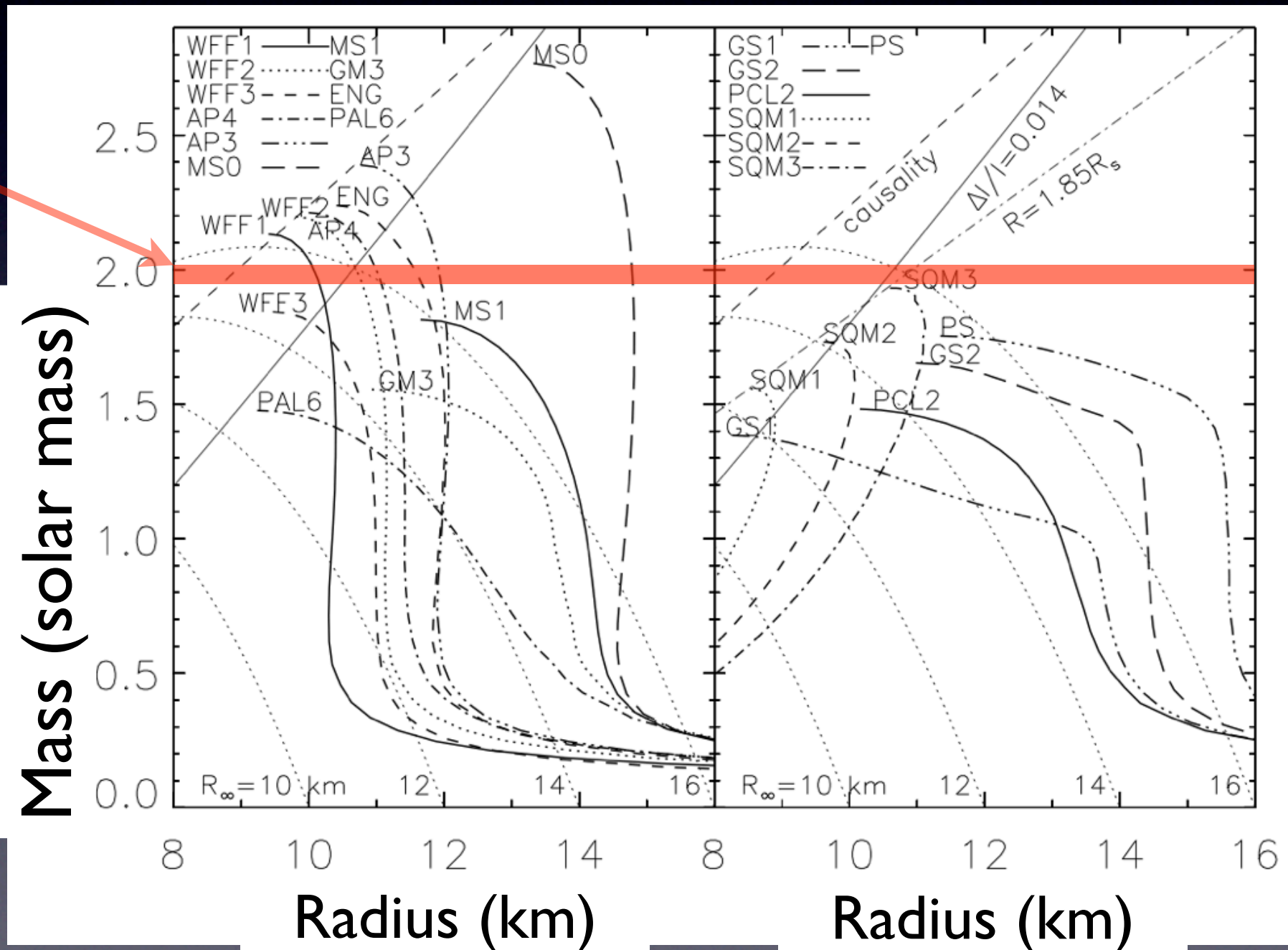


Dense Matter Equation of State

PSR J1614-2230

Mass measurement
with Shapiro Delay:
 $M_{\text{PSR}} = 1.97 \pm 0.04 M_{\odot}$

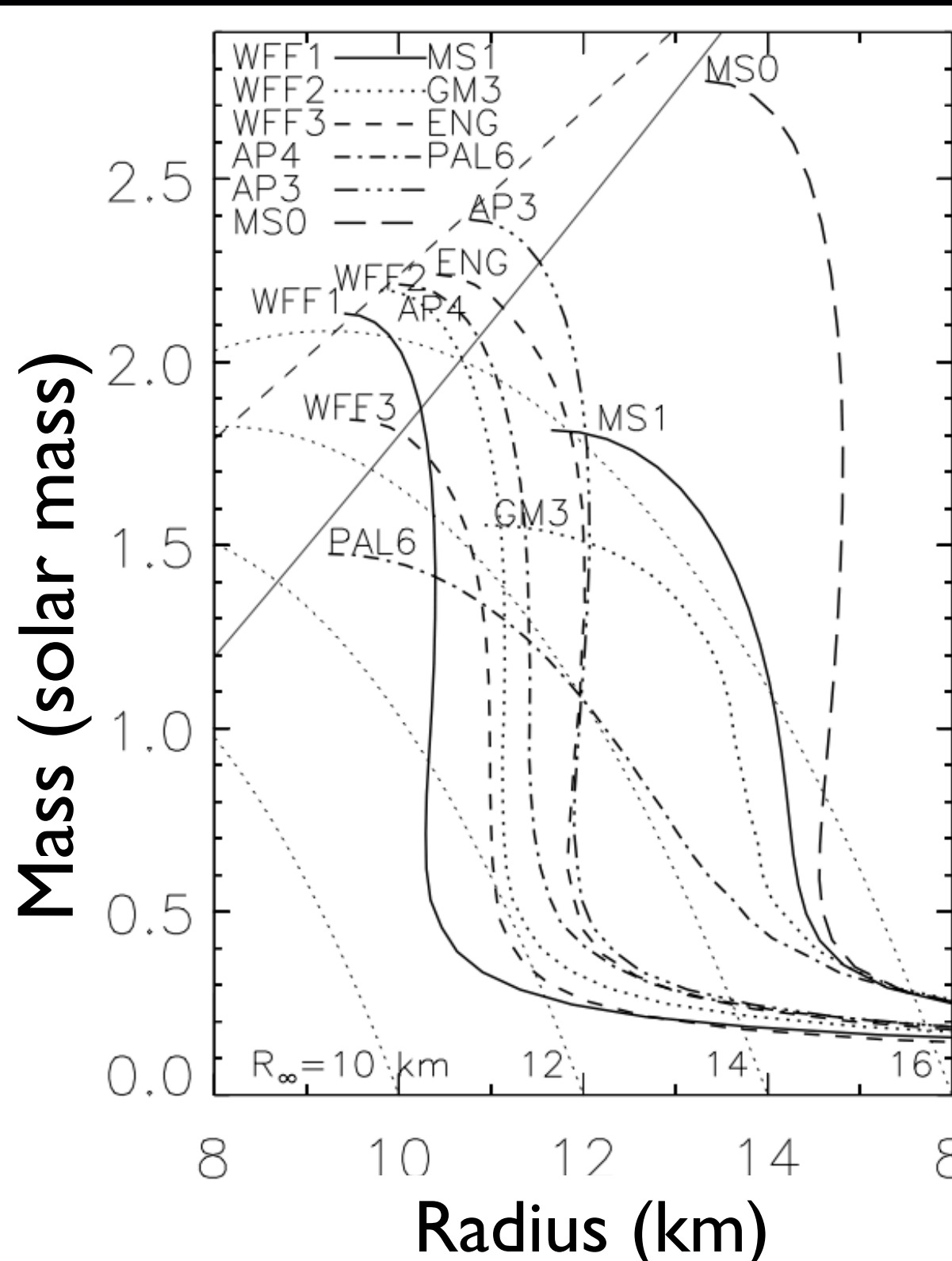
Disfavors hybrid
and quark matter
equations of state



Assumption

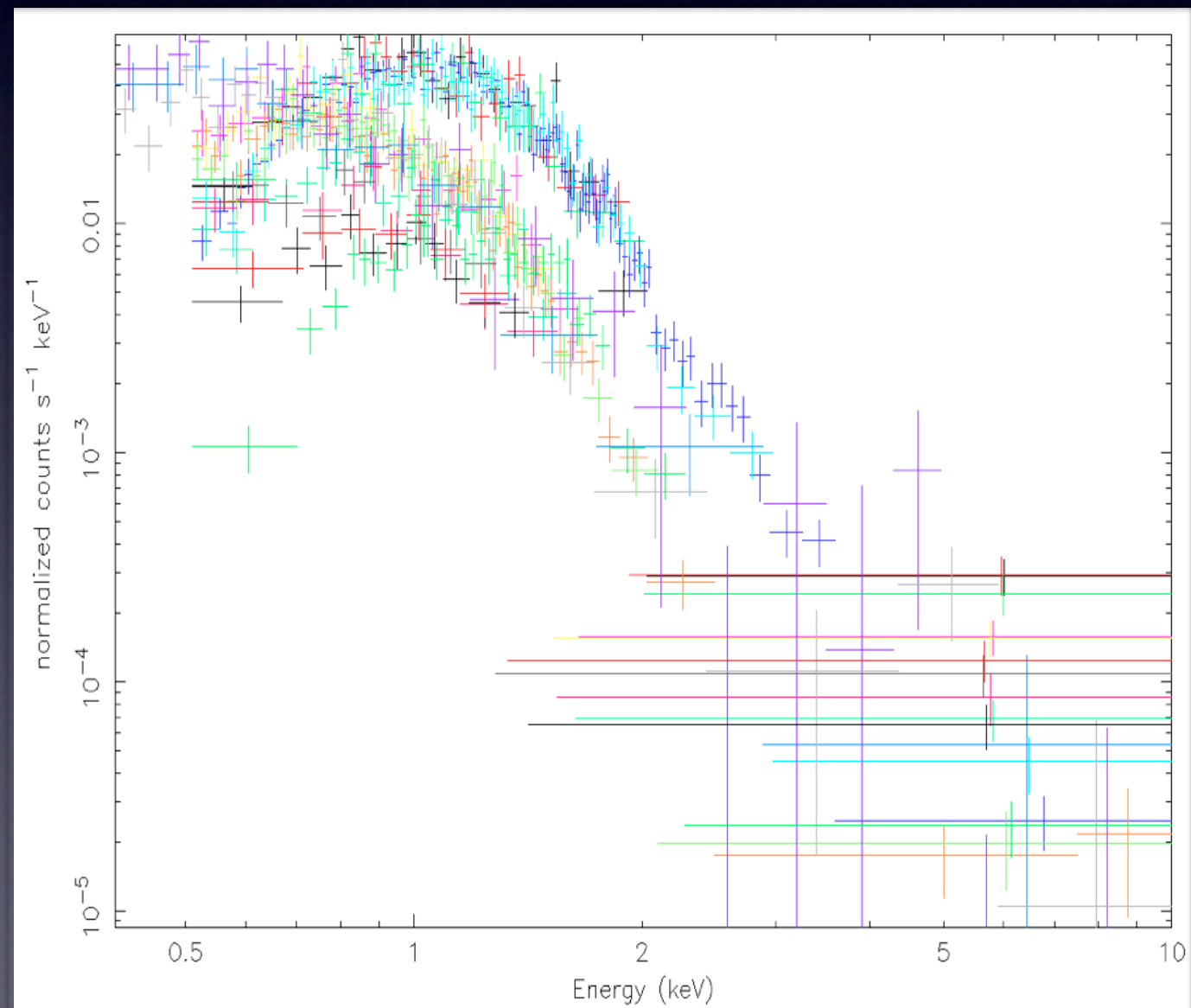
All Neutron Stars have the same radius (within $\sim 10\%$) for a wide range of masses.

We apply this assumption to the spectral fitting of a group of qLMXBs with the **nsatmos** H-atmosphere model (Heinke et al. 2006), by constraining the R_{NS} to be the same for all.



Simultaneous Spectral Fit

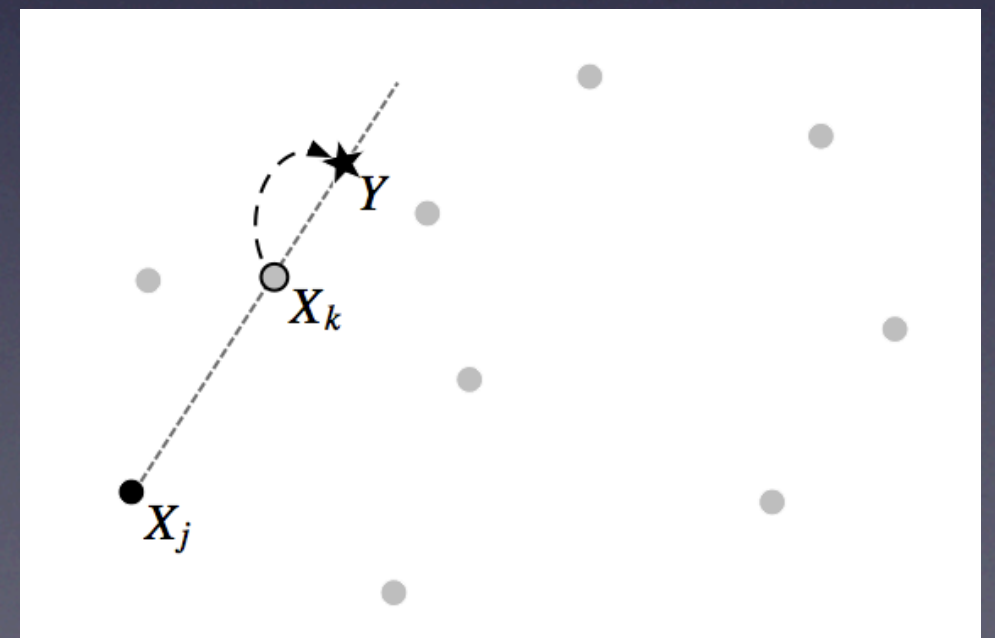
- Fit 5 qLMXBs simultaneously (M28, NGC6397, M13, ω Cen and NGC6304) with one single value of R_{NS}
- Up to 5 free parameters per target: kT_{eff} , M_{NS} , N_H , Distance, power-law component
- Up to 27 free parameters



Markov Chain Monte Carlo Simulations

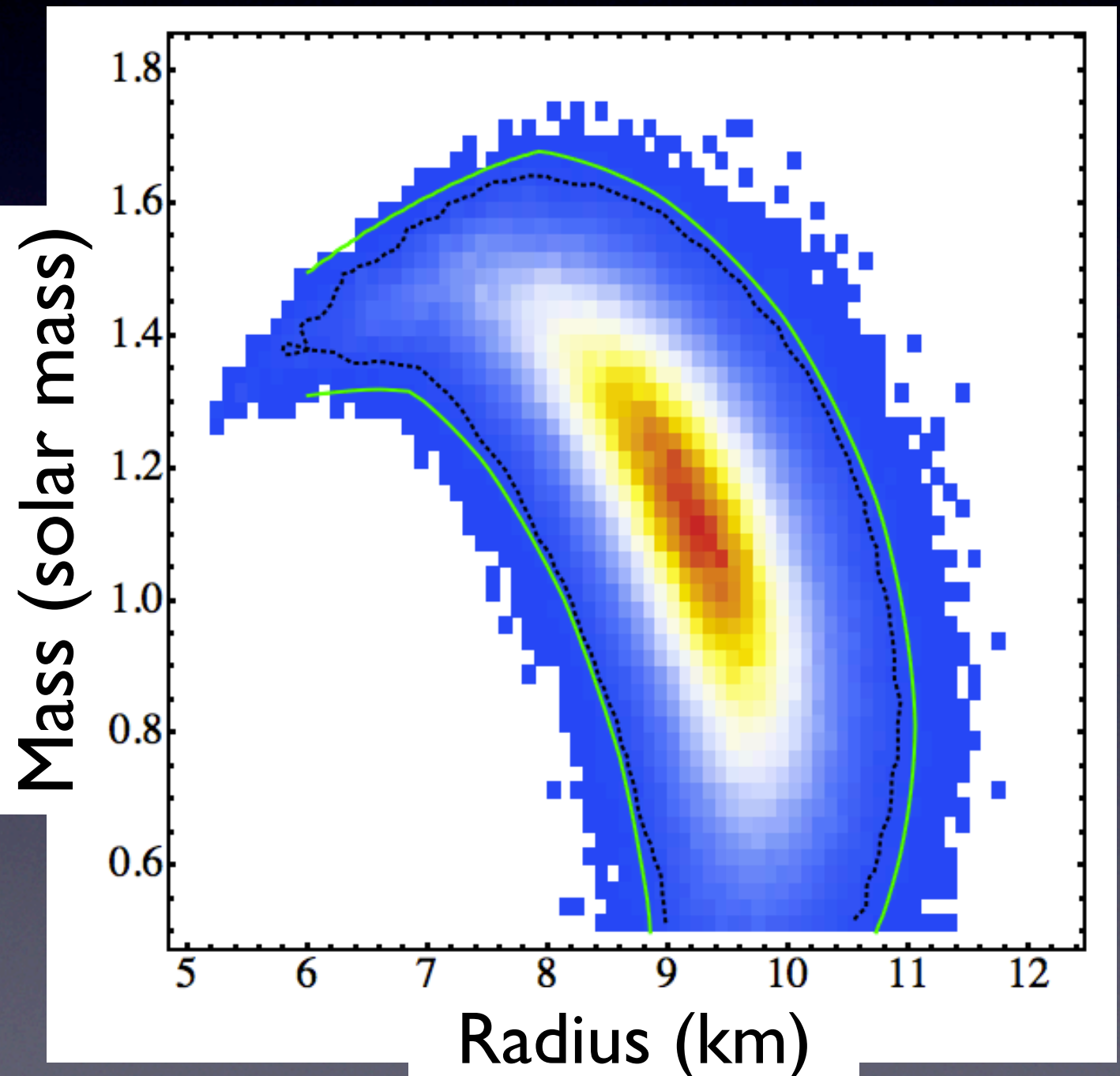
- Because the parameter space has many local minima that XSPEC struggles to identify
- Because one can include Bayesian priors for the distances
- Because one can easily obtain the marginalized posterior distribution for each parameter

We use the “Stretch-Move” algorithm, instead of Metropolis-Hasting, because it is more appropriate (faster convergence) for elongated and curved distributions



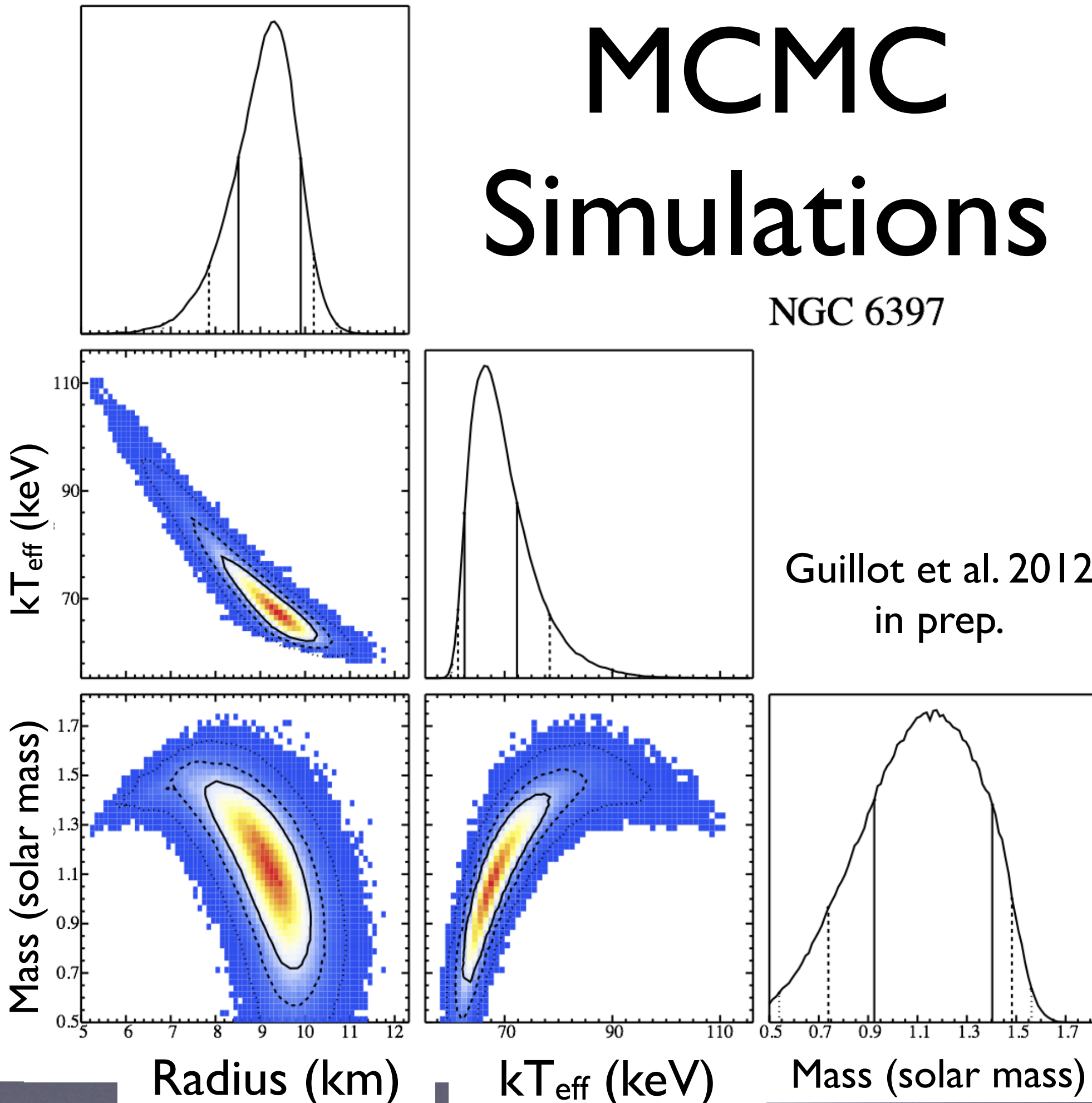
Markov Chain Monte Carlo Simulations

The MCMC approach is first tested with one single qLMXB (U24 in NGC 6397), in order to compare to XSPEC spectral analysis.



MCMC Simulations

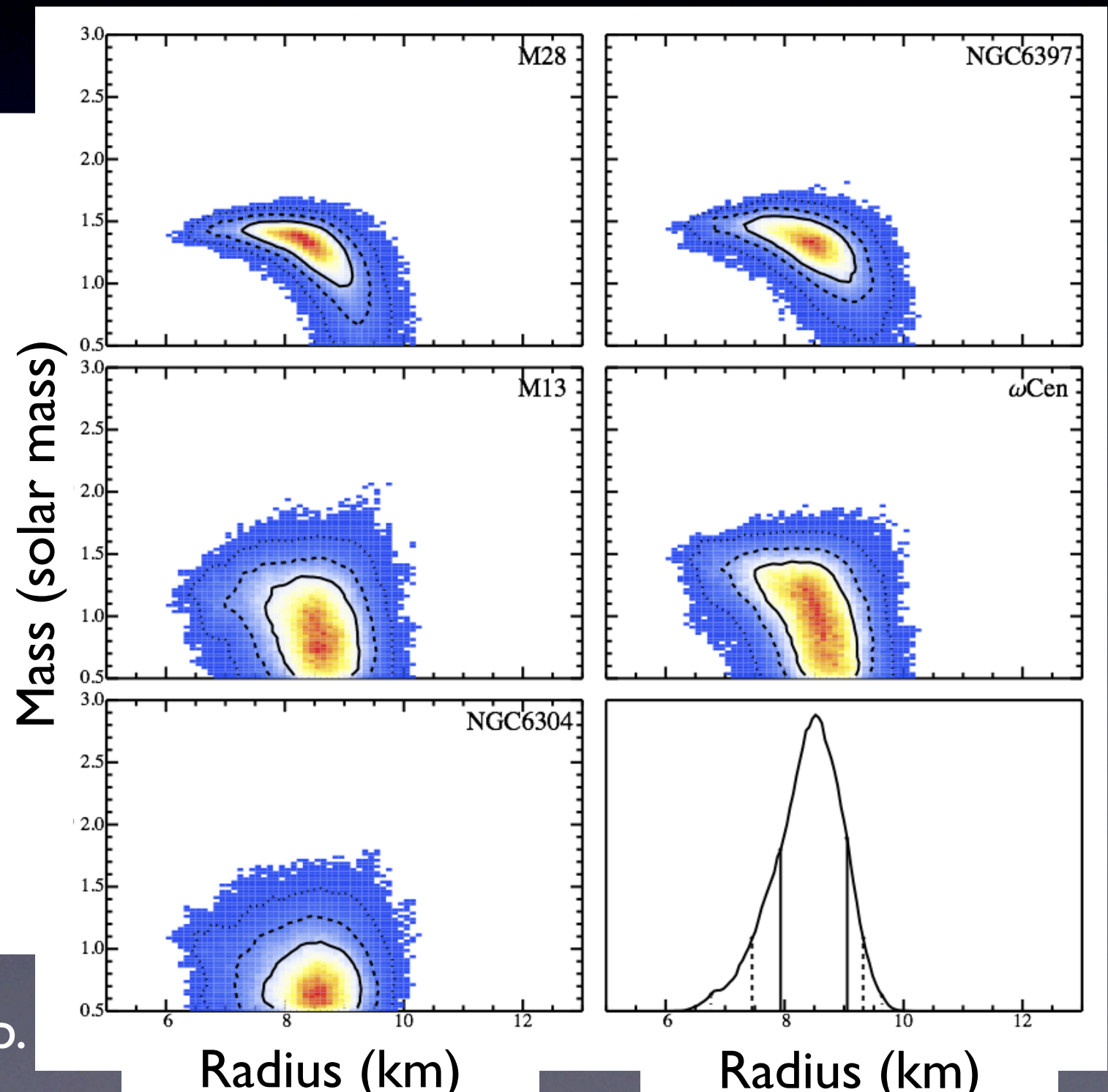
NGC 6397



Markov Chain Monte Carlo Simulations

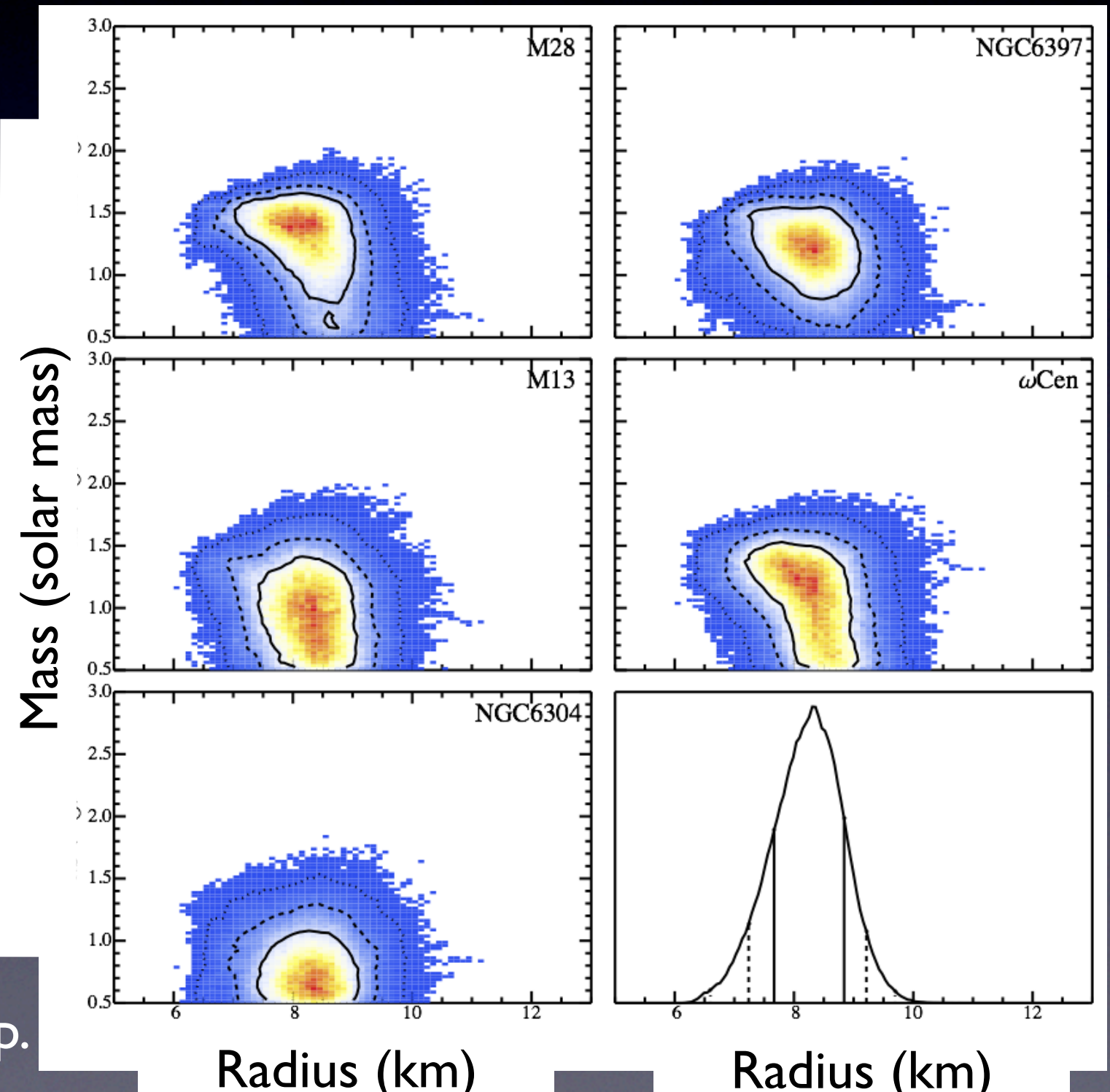
We run several simulations progressively relaxing all assumptions:

- Galactic absorption N_H
- Distances to clusters
- possible presence of a power-law component



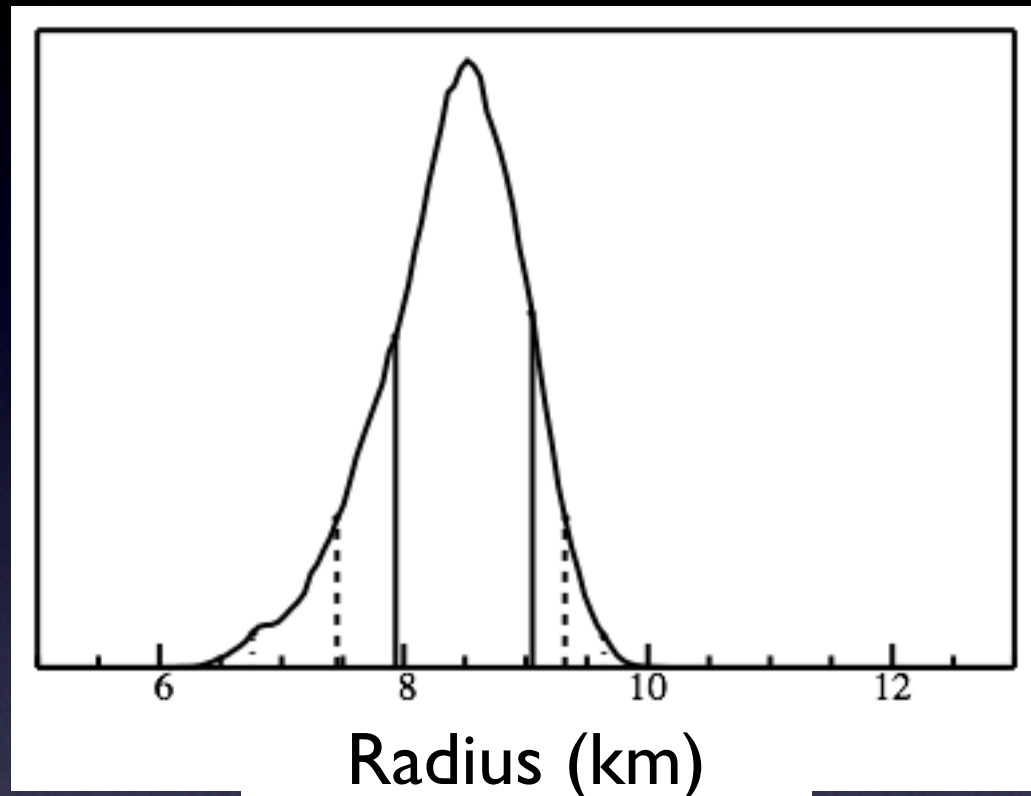
Markov Chain Monte Carlo Simulations

When we add distance priors (instead of keeping the distances fixed), the posterior distributions are broader in the R_∞ direction



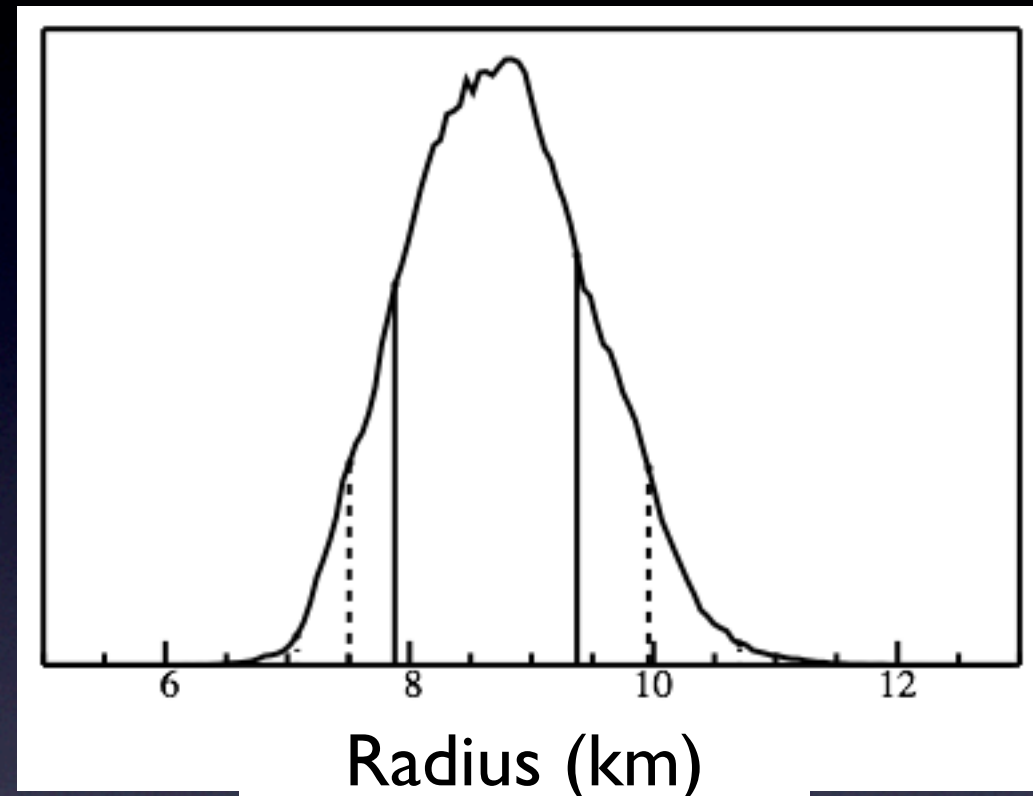
R_{NS} Measurement

Guillot et al. 2012, in prep.



Fixed N_H , Fixed distances,
no power-law added

$$R_{NS} = 8.5^{+0.8}_{-1.1} \text{ km} \\ \text{(90\%-confidence)}$$

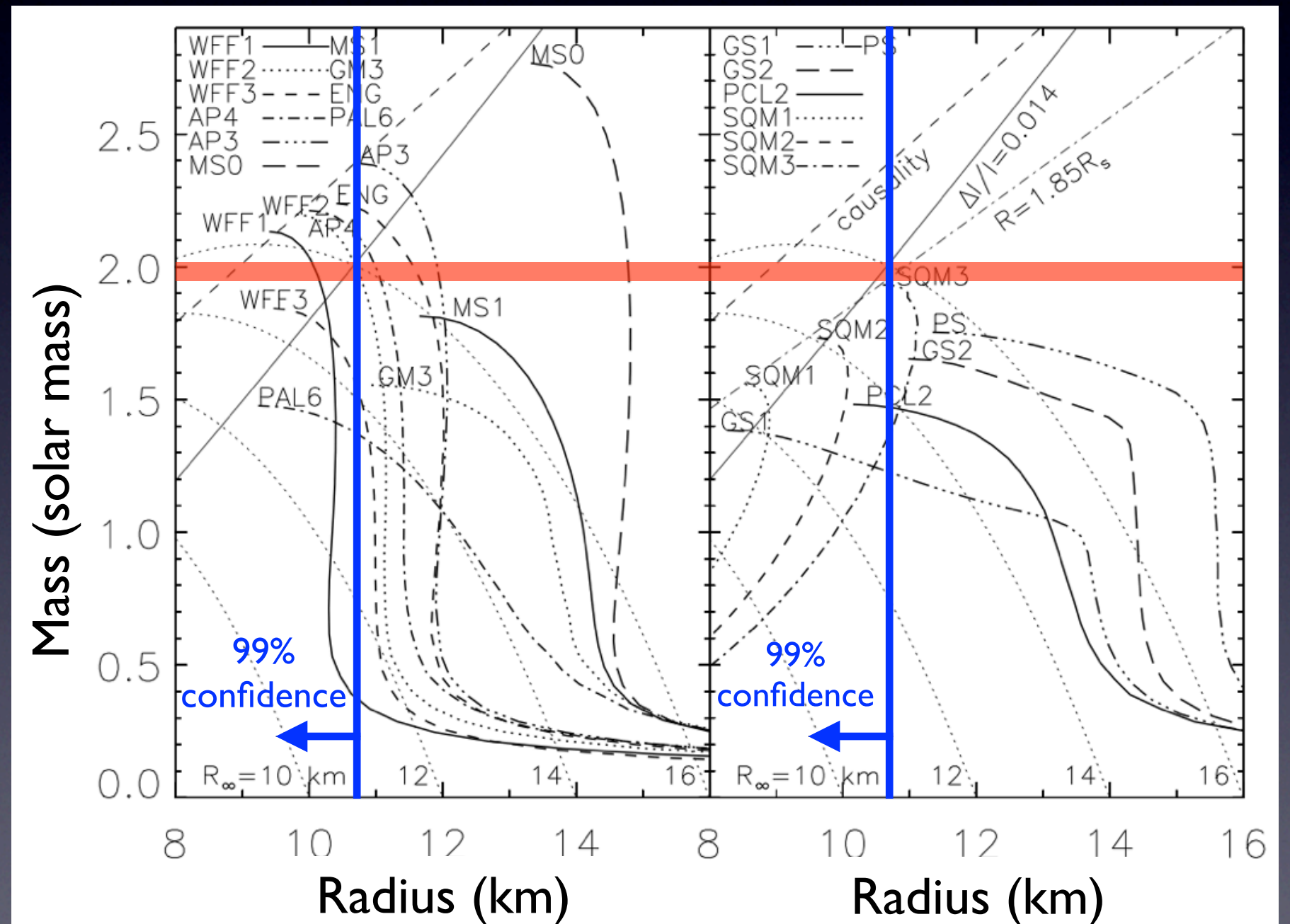


Free N_H , Bayesian priors
on distances, with power-
law component added

$$R_{NS} = 8.8^{+1.1}_{-1.3} \text{ km} \\ \text{(90\%-confidence)}$$

Constraints on Equation of State

$R_{NS} < 10.7$ km
at the 99%-
confidence level



Conclusion

- Evidence that R_{NS} is constant for a wide range of masses
- Use that assumption to measure R_{NS} from five quiescent low-mass X-ray binaries in globular clusters
- Spectral fit with *nsatmos* model using an MCMC simulation to obtain posterior distributions on each of the parameters (up to 27 free parameters)
- Measurement of $R_{\text{NS}} < 10.7$ km (99%-confidence) with the least number of assumptions, and a particular effort to control systematic uncertainties
- Only some EoSs are consistent with this results, for example, WFFI (Wiringa et al 1988)